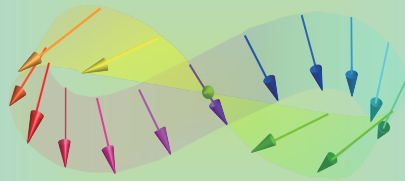


Information Storage and Spintronics

02



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14:00 Thursday, 06/October/2022 (SLB 101)



Contents of Information Storage and Spintronics

Lectures : Atsufumi Hirohata (atsufumi.hirohata@york.ac.uk, P/Z 019)
Advancement in **information storages** and spintronics (Weeks 2 ~ 9)

All lectures will be uploaded weekly in advance at

<http://www-users.york.ac.uk/~ah566/lectures/lectures.html>

14:00 ~ 15:00 Mons. (SLB 101)

14:00 ~ 15:00 Thus. (SLB 101)

- I. Introduction to information storage (01 & 02)
- II. **Magnetic information storages** (03 ~ 06)
- III. **Solid-state information storages** (07 ~ 11)
- IV. **Spintronic devices** (12 ~ 18)

Practicals :

Analysis on a spintronic device using VSM, EDX, MFM and MR (Weeks 3 ~ 8)
Operation, data and instruction will be uploaded weekly in advance at

Internal Wiki page &

<http://www-users.york.ac.uk/~ah566/lectures/lectures.html>

13:00 ~ 15:00 Weds. (P/A 016, Nanocentre and P/Z 008)

Continuous Assessment :

Assignment to be submitted via VLE (Week 10).



Quick Review over the Last Lecture

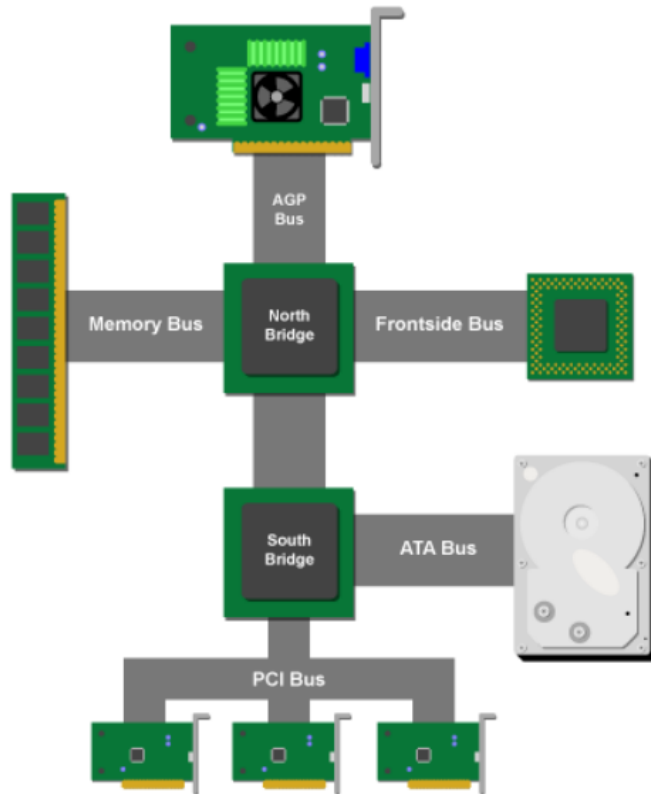
Von Neumann's model :

-
-
-
-
-

Bit / byte :

- 1 bit :
 - 2 = combinations
 - digit in binary number
- 1 byte (B) = bit

Memory access :



* http://testbench.in/introduction_to_pci_express.html;

02 Binary Data

- Binary numbers
 - Conversion
 - Advantages
- Logical conjunctions
 - Adders
 - Subtractors



Bit and Byte

Bit :

"Binary digit" is a basic data size in information storage.

1 bit : 2 = combinations ; digit in binary number

2 2 =

3 2 =

4 2 =

: : : :

Byte :

A data unit to represent one letter in Latin character set.

1 byte (B) = bit

1 kB = 1 B ×

1 MB = 1 kB ×

: :



Binary Numbers

The modern binary number system was discovered by Gottfried Leibniz in 1679 : *

Decimal notation	Binary notation
------------------	-----------------

0

1

2

3

4

5

6

7

8

: :





Conversion to Binary Numbers 1

For example, 1192 :

$$2 \overline{) 1192} \quad 1192 = 2^0 \times$$

$$2 \overline{) \underline{586} \dots 0} \quad 1192 = 2^1 \times$$

$$2 \overline{) \underline{293} \dots 0} \quad 1192 = 2^2 \times$$

$$2 \overline{) \underline{146} \dots 1} \quad 1192 = 2^3 \times$$

$$2 \overline{) \underline{73} \dots 0} \quad 1192 = 2^4 \times$$

$$2 \overline{) \underline{36} \dots 1} \quad 1192 = 2^5 \times$$

$$2 \overline{) \underline{18} \dots 0} \quad 1192 = 2^6 \times$$

$$2 \overline{) \underline{9} \dots 0} \quad 1192 = 2^7 \times$$

$$2 \overline{) \underline{4} \dots 1} \quad 1192 = 2^8 \times$$

$$2 \overline{) \underline{2} \dots 0} \quad 1192 = 2^9 \times$$

$$2 \overline{) \underline{1} \dots 0} \quad 1192 = 2^{10} \times$$

$$2 \overline{) \underline{0} \dots 1} \quad 1192_{10} = 10010010100_2$$

3



Conversion to Binary Numbers 2

For example, 0.1 :

$$0.1$$

$$0.1 \times 2 =$$

$$0.2 \times 2 =$$

$$0.4 \times 2 =$$

$$0.8 \times 2 =$$

$$0.6 \times 2 =$$

$$0.2 \times 2 =$$

:

:

$$0.1_{10} = 0.00011_2$$



Why Are Binary Numbers Used ?

In order to represent a number of "1192" by ON / OFF lamps :

Binary number : 10010010100_2 (10 digits = 10 lamps)

Decimal number : 1192_{10} (4 digits \times = 4 lamps)

Similarly, Ternary number : 1122011_3 (7 digits \times = 7 lamps)

$$\begin{aligned} 1192 &= 729 + 243 + 162 + 54 + 0 + 3 + 1 \\ &= 3^6 \times 1 + 3^5 \times 1 + 3^4 \times 2 + 3^3 \times 2 + 3^2 \times 0 + 3^1 \times 1 + 3^0 \times 1 \end{aligned}$$

Quaternary number : 112220_4 (6 digits \times = 6 lamps)

$$\begin{aligned} 1192 &= 1024 + 0 + 128 + 32 + 8 + 0 \\ &= 4^5 \times 1 + 4^4 \times 1 + 4^3 \times 2 + 4^2 \times 2 + 4^1 \times 2 + 4^0 \times 0 \end{aligned}$$

Binary numbers use the

!



Mathematical Explanation

In a base- n positional notation, a number x can be described as :

$$x = n^y \quad (y: \text{number of digits for a very simple case})$$

In order to minimise the number of devices, *i.e.*, $n \times y$,

$$\ln(x) =$$

Here, $\ln(x)$ can be a constant C ,

$$C =$$

$$y =$$

By substituting this relationship into $n \times y$,

$$n \times y =$$

To find the minimum of $n / \ln(n)$,

$$[n / \ln(n)]' =$$

Here, $[n / \ln(n)]' = 0$ requires

$$= 0$$

Therefore, $n =$

provides the minimum number of devices.



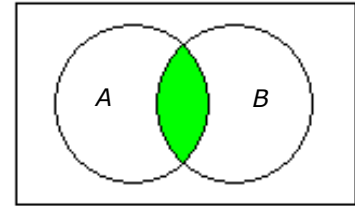
Logical Conjunctions 1

AND :

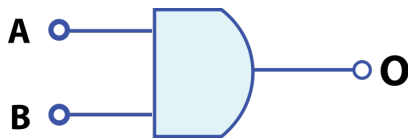
Venn diagram of $A \wedge B$

Truth table

Input		Output
A	B	$A \wedge B$
True (T) (1)	T (1)	
False (F) (0)	T (1)	
T (1)	F (0)	
F (0)	F (0)	



Logic circuit



* <http://www.wikipedia.org/>



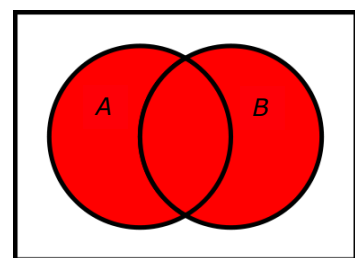
Logical Conjunctions 2

OR :

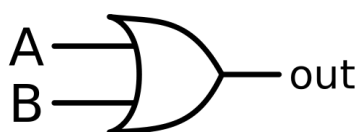
Venn diagram of $A \vee B$

Truth table

Input		Output
A	B	$A \vee B$
T (1)	T (1)	
F (0)	T (1)	
T (1)	F (0)	
F (0)	F (0)	



Logic circuit



* <http://www.wikipedia.org/>



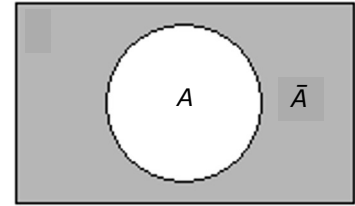
Logical Conjunctions 3

NOT :

Venn diagram of \bar{A}

Truth table

Input	Output
A	\bar{A}
T (1)	
F (0)	



Logic circuit



* <http://www.wikipedia.org/>



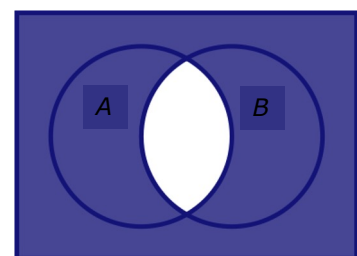
Additional Logical Conjunctions 1

NAND = (NOT A) OR (NOT B) = NOT (A AND B) :

Venn diagram of $A \uparrow B$

Truth table

Input		Output
A	B	$A \uparrow B$
T (1)	T (1)	
F (0)	T (1)	
T (1)	F (0)	
F (0)	F (0)	



Logic circuit



* <http://www.wikipedia.org/>



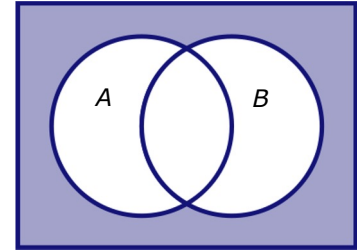
Additional Logical Conjunctions 2

NOR = NOT (A OR B) :

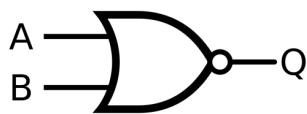
Venn diagram of $A \downarrow B$

Truth table

Input		Output
A	B	$A \downarrow B$
T (1)	T (1)	
F (0)	T (1)	
T (1)	F (0)	
F (0)	F (0)	



Logic circuit



NOR can represent all the logical conjunctions :

- NOT A =
- A AND B =
- A OR B =

* <http://www.wikipedia.org/>



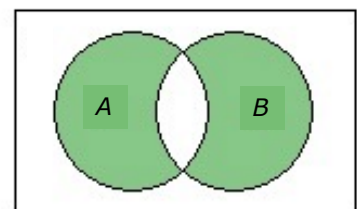
Additional Logical Conjunctions 3

XOR = Exclusive OR :

Venn diagram of $A \oplus B$

Truth table

Input		Output
A	B	$A \oplus B$
T (1)	T (1)	
F (0)	T (1)	
T (1)	F (0)	
F (0)	F (0)	



Logic circuit



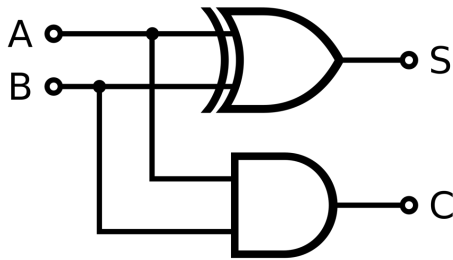
* <http://www.wikipedia.org/>



Half Adder

Simple adder for two single binary digits :

XOR for the sum (S)



AND for the carry (C), which represents the overflow for the next digit

Truth table

Input		Output	
A	B	S	C
1	1		
0	1		
1	0		
0	0		

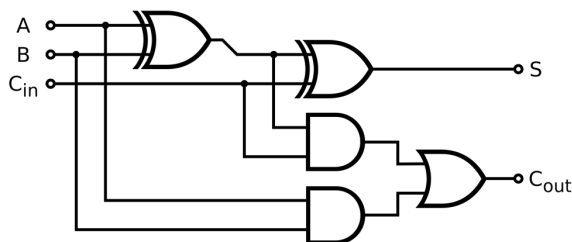
* <http://www.wikipedia.org/>



Full Adder

Adder for two single binary digits as well as values carried in (C_{in}) :

2 half adders for sum (S)



Additional OR for the carry (C_{out}), which represents the overflow for the next digit

Truth table

Input			Output	
A	B	C_{in}	S	C_{out}
1	1	1		
0	1	1		
1	0	1		
0	0	1		
1	1	0		
0	1	0		
1	0	0		
0	0	0		

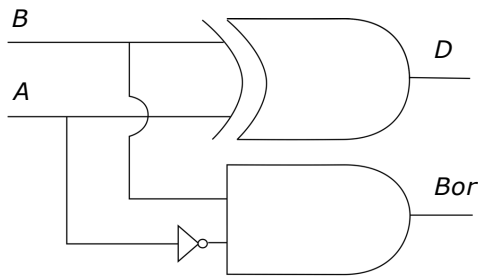
* <http://www.wikipedia.org/>



Half Subtractor

Simple subtractor for two single binary digits, minuend (A) and subtrahend (B) :

XOR for the difference (D)



NOT and AND for the borrow (Bor), which is the borrow from the next digit

Truth table

Input		Output	
A	B	D	Bor
1	1		
0	1		
1	0		
0	0		

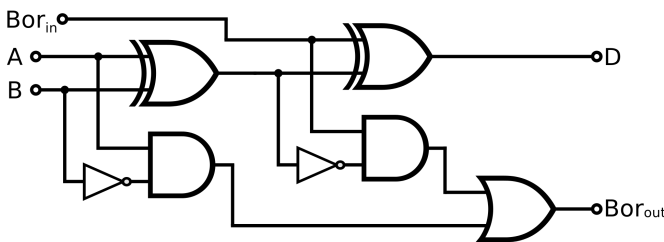
* <http://www.wikipedia.org/>



Full Subtractor

Subtractor for two single binary digits as well as borrowed values carried in (Bor_{in}) :

2 half subtractor for difference (D)



Additional OR for the borrow (Bor_{out}), which is the borrow from the next digit

Truth table

Input			Output	
A	B	Bor_{in}	D	Bor_{out}
1	1	1	1	1
0	1	1	0	1
1	0	1	0	0
0	0	1	1	1
1	1	0	0	0
0	1	0	1	1
1	0	0	1	0
0	0	0	0	0

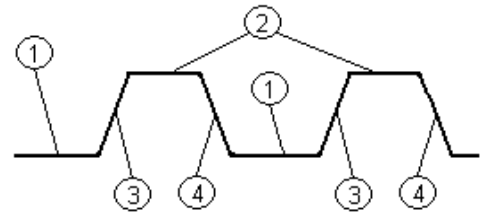
* <http://www.wikipedia.org/>



Information Processing

For data processing, two distinct voltages are used to represent "1" and "0" :

Low level (1) and high level (2) voltages



Voltages used :

Devices	Low voltage	High voltage
Emitter-coupled logic (ECL)	- 5.2 ~ 1.175 V	0 ~ 0.75 V
Transistor-transistor logic (TTL)	0 ~ 0.8 V	2 ~ 4.75 (or 5.25) V
Complementary metal-oxide-semiconductor (CMOS)	0 ~ $V_{DD} / 2$	$V_{DD} / 2 \sim V_{DD}$ ($V_{DD} = 1.2, 1.8, 2.4, 3.3$ V etc.)

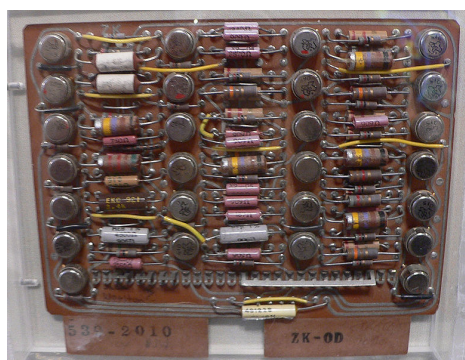
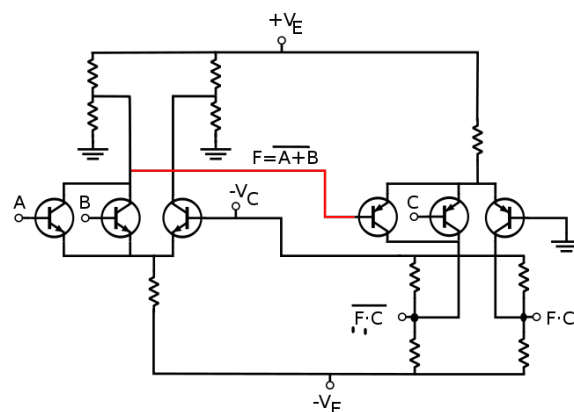
* <http://www.wikipedia.org/>



Emitter-Coupled Logic

In 1956, Hannon S. Yourke invented ECL at IBM : *

High-speed integrated circuit, differential amplifier, with bipolar transistors



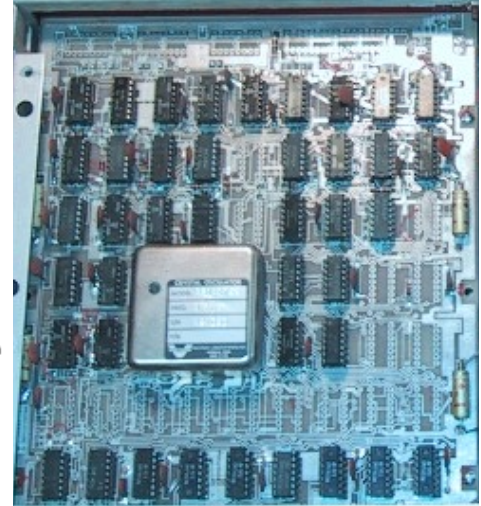
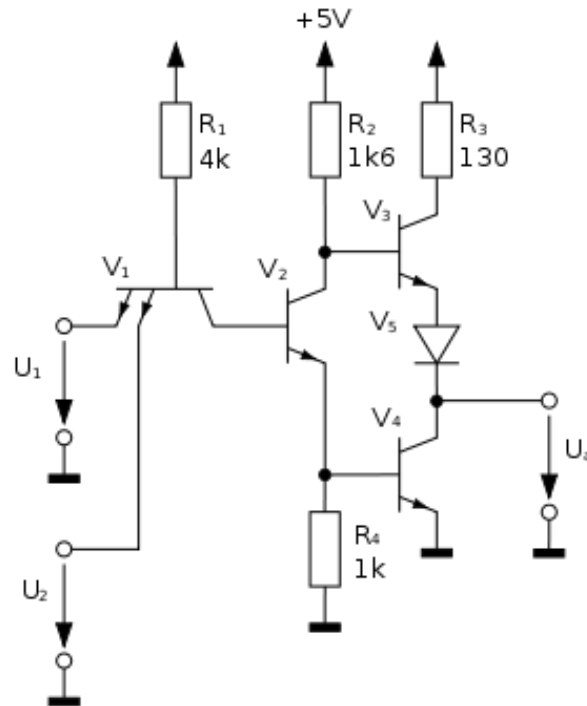
* <http://www.wikipedia.org/>



Transistor-Transistor Logic

In 1961, James L. Buie invented TTL at TRW : *

Integrated circuit, logic gate and amplifying functions with bipolar transistors



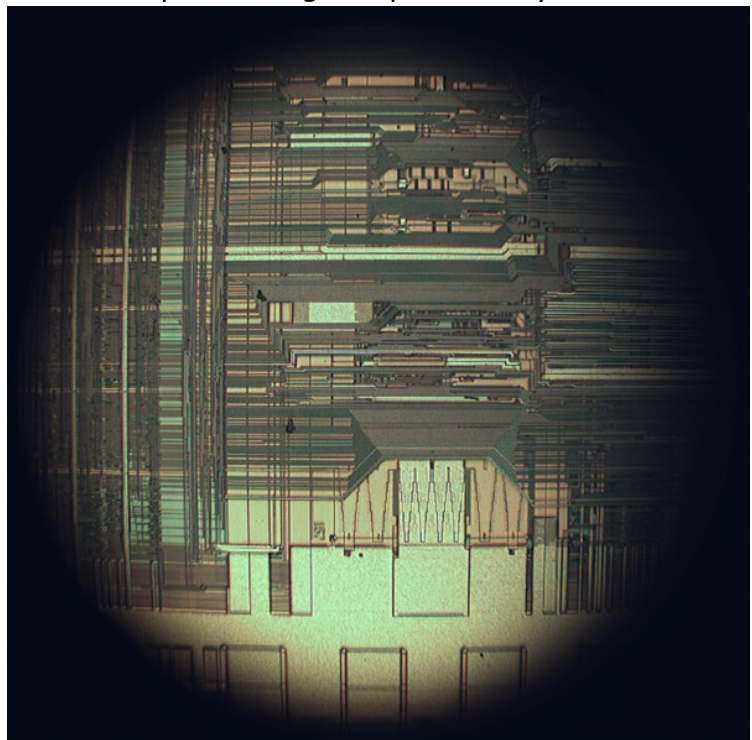
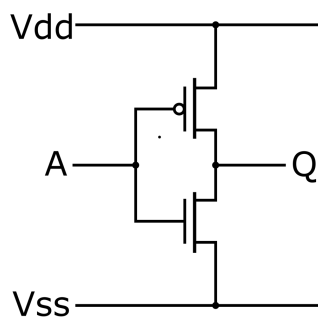
* <http://www.wikipedia.org/>



Complementary Metal-Oxide-Semiconductor

In 1963, Frank Wanlass patented CMOS : *

Integrated circuit with low power consumption using complementary MOSFET



* <http://www.wikipedia.org/>