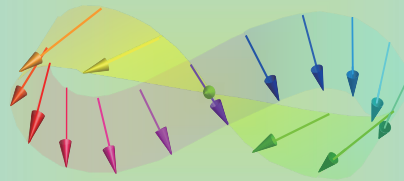


# Nanoelectronics 18



Atsufumi Hirohata

*Department of Electronic Engineering*

THE UNIVERSITY *of York*



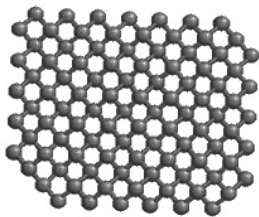
12:00 Thursday, 16/March/2023 (P/T 005A)



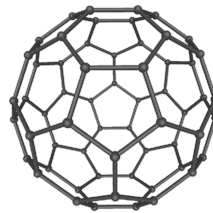
## Quick Review over the Last Lecture

Carbon nanomaterials :

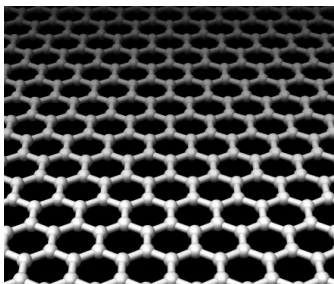
( ): :



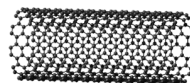
( ): :



( ): :



( ): :





# Contents of Nanoelectronics

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- I. Introduction to Nanoelectronics (01)
  - 01 Micro- or nano-electronics ?
- II. Electromagnetism (02 & 03)
  - 02 Maxwell equations
  - 03 Scalar and vector potentials
- III. Basics of quantum mechanics (04 ~ 06)
  - 04 History of quantum mechanics 1
  - 05 History of quantum mechanics 2
  - 06 Schrödinger equation
- IV. Applications of quantum mechanics (07, 10, 11, 13 & 14)
  - 07 Quantum well
  - 10 Harmonic oscillator
  - 11 Magnetic spin
  - 13 Quantum statistics 1
  - 14 Quantum statistics 2
- V. Nanodevices (08, 09, 12, 15 ~ 18)
  - 08 Tunnelling nanodevices
  - 09 Nanomeasurements
  - 12 Spintronic nanodevices
  - 15 Low-dimensional nanodevices
  - 16 Optical nanodevices
  - 17 Organic nanodevices
  - 18 Quantum computation

## 18 Quantum Computation

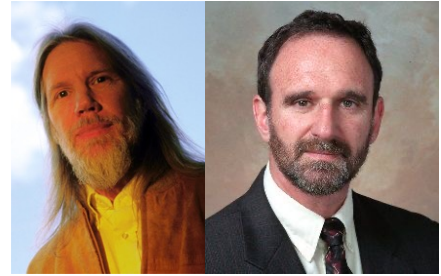
- Public key cryptosystem
- Traveling salesman problem
  - Qubits



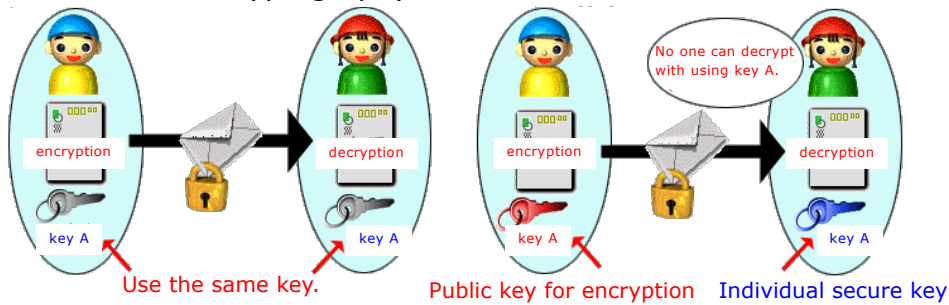
# Public Key Cryptosystem

In 1976, B. Whitfield Diffie and Martin E. Hellman proposed public key cryptosystem.

RSA (Ronald L. Rivest, Adi Shamir and Leonard M. Adleman) cryptography developed in 1977.



## Conventional cryptography



256-digit factorization :

BUT ~

with IBM Blue Gene

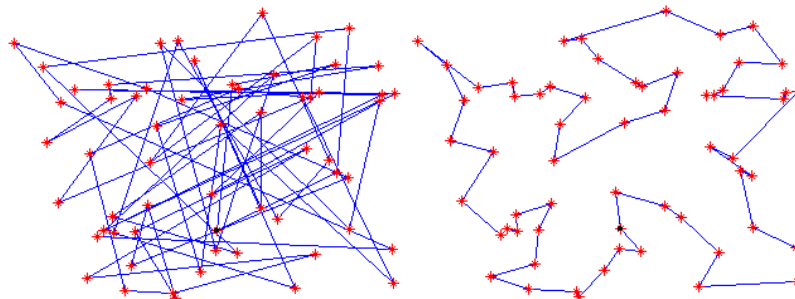
with a quantum computer !

\* <http://www.wikipedia.org/>  
\*\* <http://www.maitou.gr.jp/rsa/>



# Traveling Salesman Problem

As an example of non-deterministic polynomial (NP) complete problems :



\* <http://www.wikipedia.org/>



# Bee Can Solve a Traveling Salesman Problem

guardian.co.uk

## Bees' tiny brains beat computers, study finds

Bees can solve complex mathematical problems which keep computers busy for days, research has shown

- In pictures: [Why the decline in bees matters](#)
- [Fears for crops as shock figures from America show scale of bee catastrophe](#)

Press association  
guardian.co.uk, Sunday 24 October 2010 21:45 BST



Researchers found that bees could solve the 'travelling salesman's' shortest route problem, despite having a brain the size of a grass seed. Photograph: Rex Features



# History of Quantum Computation

In 1956, Richard P. Feynman told :

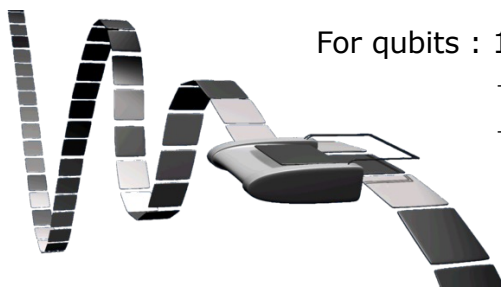
“There’s plenty of room at the bottom.”

In 1980, Paul Benioff predicted :

calculations without energy consumption  
→ quantum computation

In 1985, David Deutsch introduced quantum turing machine.

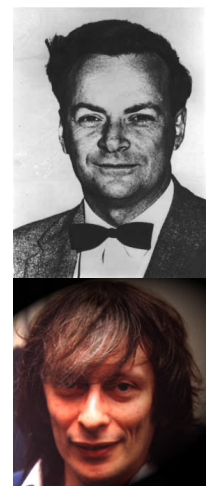
Turing machine : Input tape with letters



For qubits : 1 tape insertion

→  $2^n$  calculations achieved

→ parallel calculation



In 1994, Peter W. Shor formulated factorization algorithm.

In 1996, L. K. Grover developed database algorithm.

\* <http://www.wikipedia.org/>

\*\* K. Nakamura, *SX World* 26, Autumn (2000).



# Technical Requirements for a Quantum Computer

5 major technical obstacles for the realisation of a quantum computer : \*

Array of necessary numbers of qubits

Factorization of a 200-digit integer → 1000 qubits

Initialisation of qubits

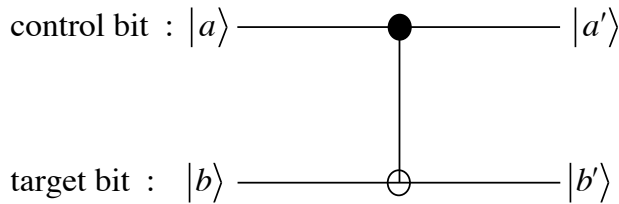
$$|0\rangle \otimes \dots \otimes |0\rangle$$

Long coherence time

Q-factor = coherence time / 1 gate time > 10,000

Operationability of a quantum logic gate

1-qubit unitary transformation + 2-qubit CNOT gate



$ a\rangle$	$ b\rangle$	$ a'\rangle$	$ b'\rangle$
$ 0\rangle$	$ 0\rangle$	$ 0\rangle$	$ 0\rangle$
$ 0\rangle$	$ 1\rangle$	$ 0\rangle$	$ 1\rangle$
$ 1\rangle$	$ 0\rangle$	$ 1\rangle$	$ 1\rangle$
$ 1\rangle$	$ 1\rangle$	$ 1\rangle$	$ 0\rangle$

Observability of qubits

\* S. Kawabata, *NRI Res. Rep.* 1, 4 (2004).



## Potential Qubits

Major potential qubits for quantum computation :

'0'	'1'	Qubit	'0'	'1'	Qubit
$ V\rangle$	$ H\rangle$	Photons Linear Polarization	$+\frac{1}{2}\hbar$	$-\frac{1}{2}\hbar$	Electron, Neutron Spin
$ L\rangle$	$ R\rangle$	Photons Circular Polarization	$ a\rangle$	$ b\rangle$	Atom: Internal States
$ b\rangle$	$ a\rangle$	Photons Linear Polarization	$ a\rangle$	$ b\rangle$	Quantum-dot Energy Levels

Qubits	Q-factor	Present records	Notes
Nuclear magnetic resonance (NMR)	$10^9$	7 qubits (algorithm)	Maximum 10 qubits
Ion-trap	$10^{12}$	2 qubits (algorithm)	Difficult to integrate
Superconducting charge	$10^4$	2 qubits (control NOT)	
Superconducting flux	$10^3$	1 qubit (unitary transformation)	
Exciton (electron-hole pair)	$10^3$	2 qubits (control NOT)	
Electron charge	$10^5$	1 qubit (unitary transformation)	
Electron spin	$10^4$		
Nuclear spin	$10^9$		

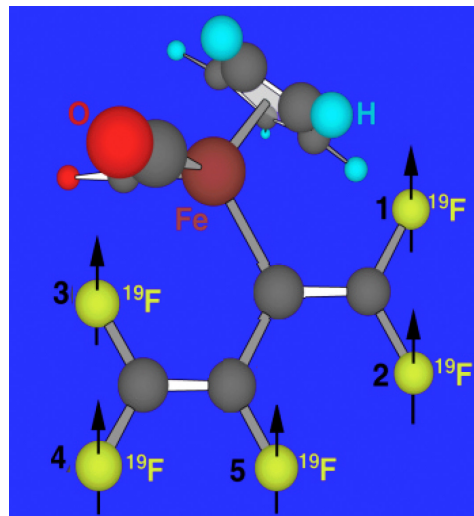
\* K. Goser, P. Glösekötter and J. Dienstuhl, *Nanoelectronics and Nanosystems* (Springer, Berlin, 2004).

\*\* S. Kawabata, *NRI Res. Rep.* 1, 4 (2004).



# NMR Qubits

5-qubit operation at 215 Hz was achieved :



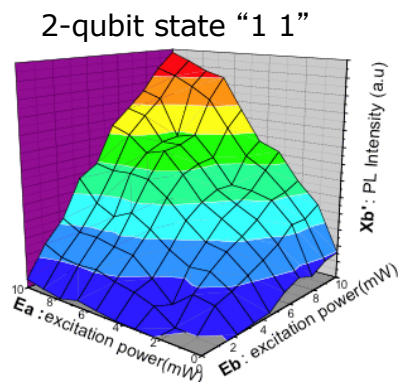
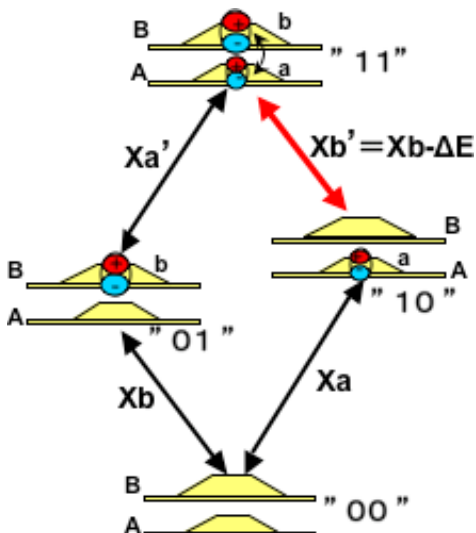
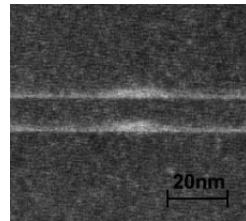
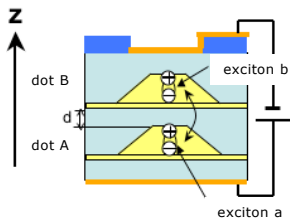
Maximum 10 qubits ...

\* L. M. K. Vandersypen *et al.*, *Phys. Rev. Lett.* **85**, 5452 (2000).



# Exciton Qubits in Solid States

InAs quantum dots buried in GaAs act as qubits :

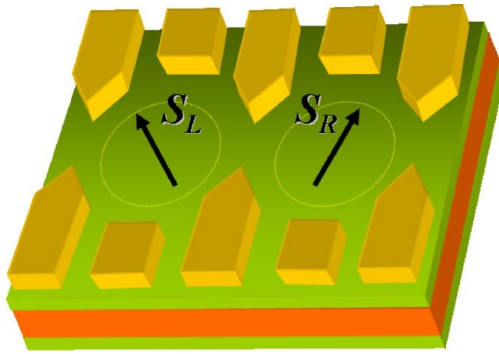


\* K. Goshima *et al.*, *Appl. Phys. Lett.* **87**, 253110 (2005).



## Spin Qubits in Solid States

In 1998, Daniel Loss and David P. DiVincenzo proposed spin qubits :



Qubits : electron spins embedded in quantum dots

Unitary transformation : application of an external magnetic field

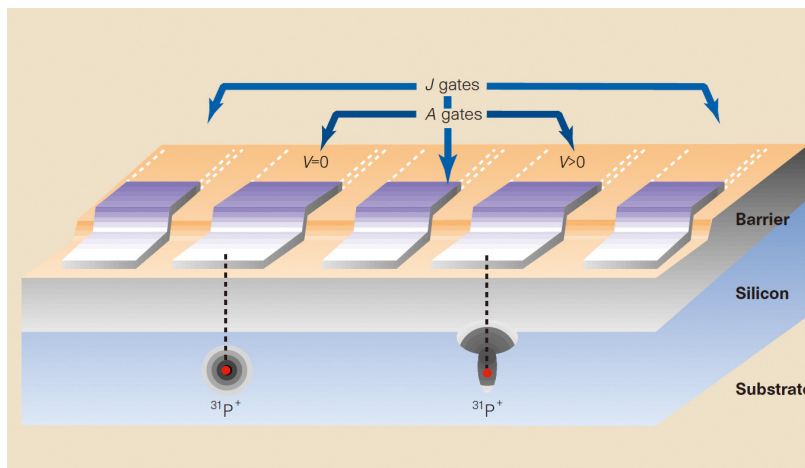
Control NOT : Heisenberg interaction between neighbouring spins

\* <http://theorie5.physik.unibas.ch/loss/>  
\*\* <http://www.rle.mit.edu/60th/speakers.htm>  
\*\*\* <http://www.wikipedia.org/>



## Nuclear Spin Qubits in Solid States

In 1998, Bruce E. Kane proposed nuclear spin qubits doped in Si :



Advantage : very long coherence time ( $10^6$  sec at  $\sim 100$  mK)

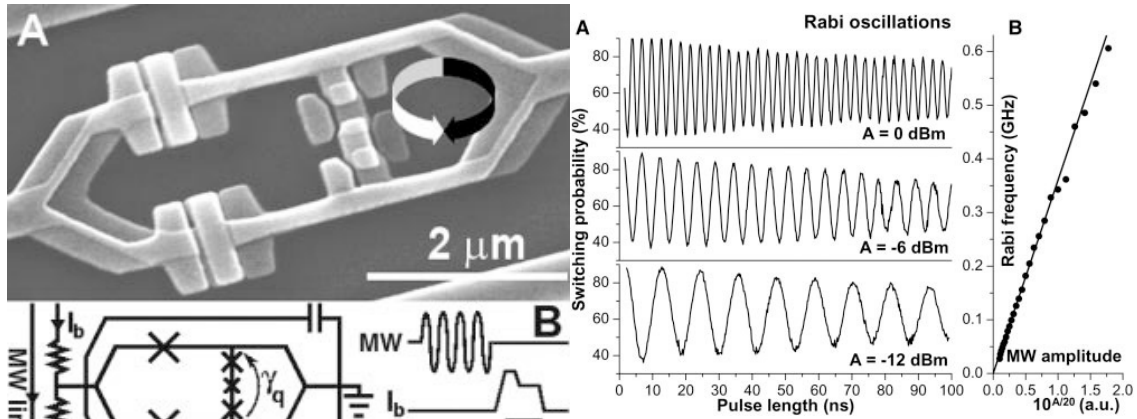
By applying gate A voltage, P<sup>+</sup> and an electron in an A gate couples  $\rightarrow$  polarises.

J gate controls the interaction between the neighbouring nuclear spins.



# Superconducting Qubits in Solid States

In 1999, first demonstration of 1-qubit unitary transformation in solid states :

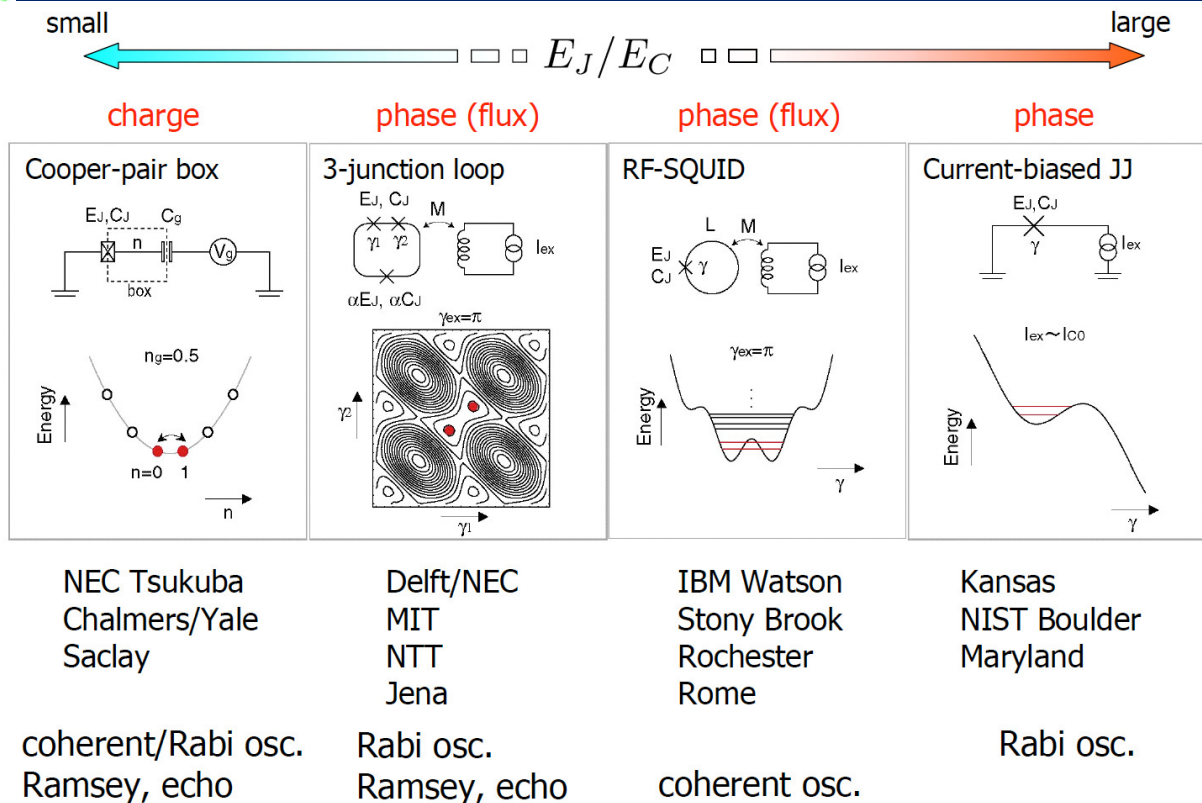


Rabi oscillation :  
Proof of quantum entanglement

\* Y. Nakamura *et al.*, *Nature* **398**, 876 (1999); I. Chiorescu *et al.*, *Science* **299**, 1869 (2003).



## Other Superconducting Qubits







# Roadmap for Quantum Computation

## D-Wave & ARDA Hardware Roadmaps

### D-Wave Roadmap

### ARDA Roadmap

# Entangled Qubits	# Qubits QFT	Year	ARDA Milestone
1 <sup>1</sup>	-	2002	
2	-	2003	
4	2	2004	
8	4	2005	
16	8	2006	
32 gates <sup>1</sup>	16	2007	3-5 qubits entangled; 2-qubit
64	32	2008	
		2009	
		2010	
		2011	
		2012	10 or more qubits entangled

<sup>1</sup> Already completed for charge (published), underway for 3J, Saclay & CBJJ qubits.

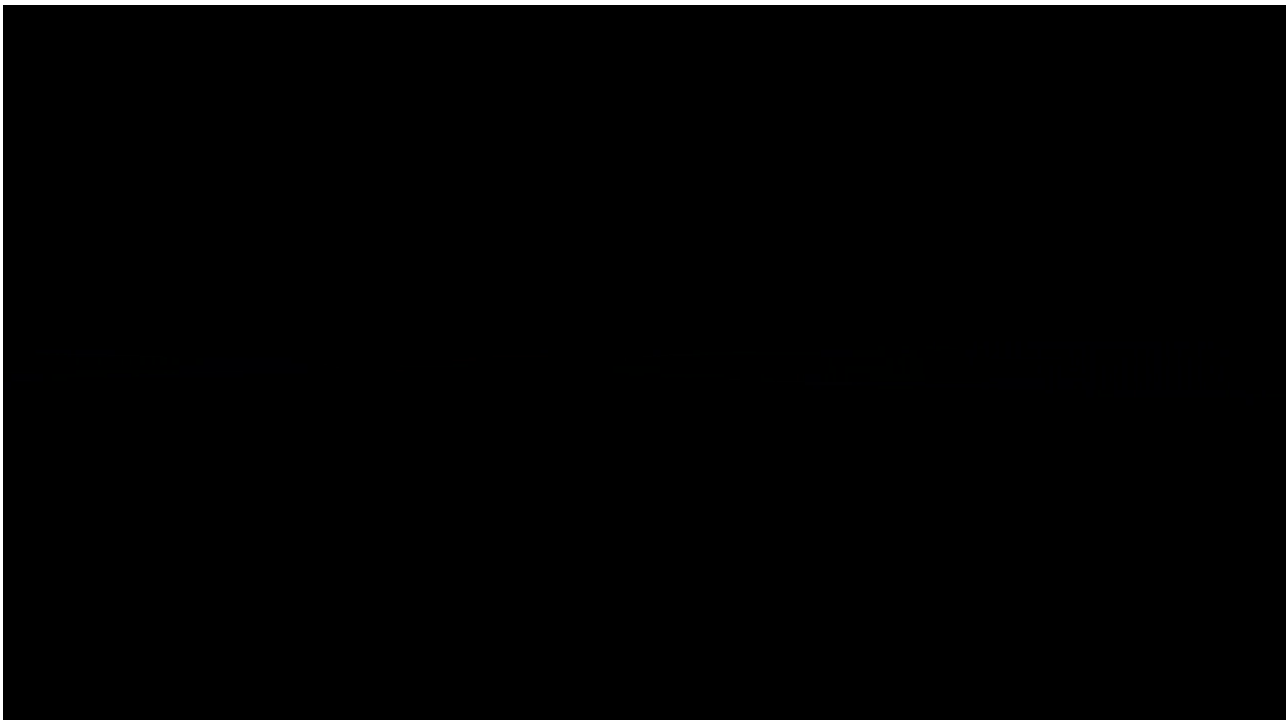
<http://www.dwavesys.com/>

<http://googleresearch.blogspot.jp/2013/05/launching-quantum-artificial.html>

\* [http://www3.fed.or.jp/salon/2ndryo/2ndryo\\_houkokusho\\_.pdf](http://www3.fed.or.jp/salon/2ndryo/2ndryo_houkokusho_.pdf)



## Quantum Annealing

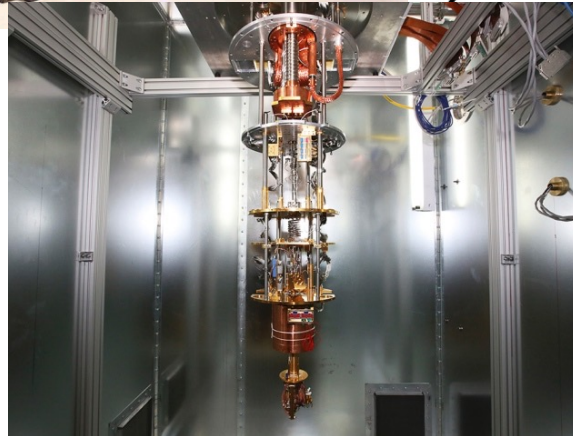
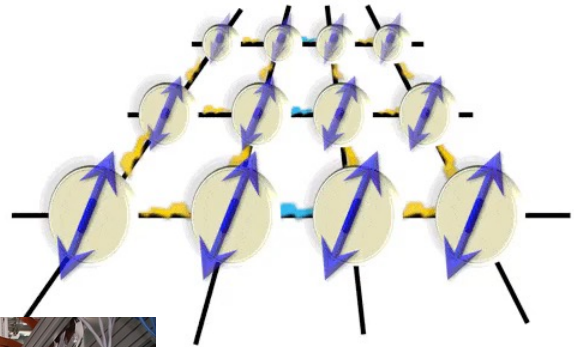


\* [https://www.youtube.com/watch?v=UV\\_RICAc5Zs](https://www.youtube.com/watch?v=UV_RICAc5Zs)



## Latest Model from D-Wave

In 2017, D-Wave introduced a 2,000 qubit system with quantum annealing :



\* E. Gibney, *Nature* 541, 447 (2017);  
\*\* <http://codezine.jp/article/detail/9491>



## Blueprint from the University of Sussex

In 2017, Sussex group proposed a trapped-ion quantum computer :



**How to construct  
a microwave trapped-ion  
quantum computer**

\* <https://www.youtube.com/watch?v=LZdJB1pryMw>



# Quantum Cryptosystem

TU Darmstadt and NIST initiated a call for cryptosystem using quantum computation :

The screenshot shows the NIST Post-Quantum Cryptography website. At the top left, there is a banner for the 'TU DARMSTADT LATTICE CHALLENGE' featuring a honeycomb pattern. Below this, the 'INTRODUCTION' section is visible, with a 'SUBMISSION' button. The main header includes the NIST logo, 'Information Technology Laboratory', and 'COMPUTER SECURITY RESOURCE CENTER'. A 'PROJECTS' button is also present. The main content area is titled 'Post-Quantum Cryptography' and includes a 'Project Overview' section. On the right, there is a 'PROJECT LINKS' sidebar with links for 'Overview', 'FAQs', 'News & Updates', 'Events', and 'Publications'.

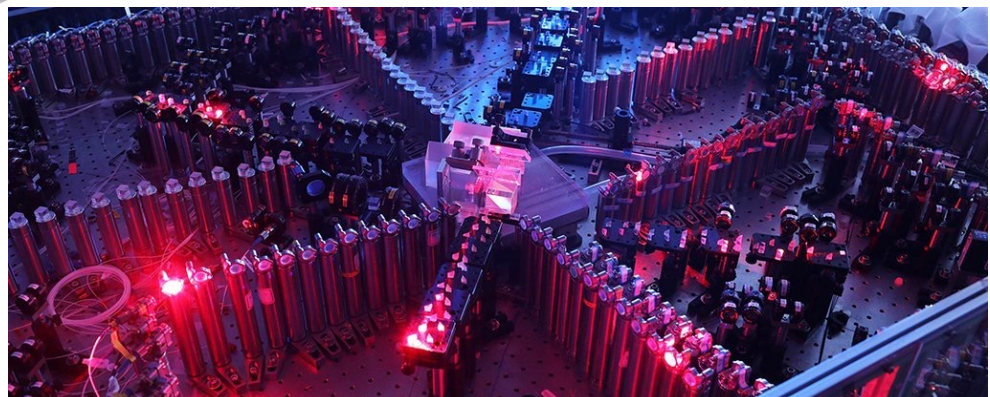
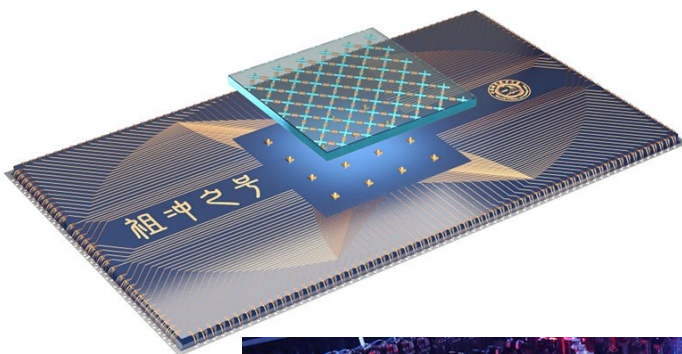
\* <https://www.latticechallenge.org>

\*\* <https://csrc.nist.gov/Projects/Post-Quantum-Cryptography/Round-1-Submissions>



# Latest Quantum Computer

University of Science and Technology of China and QuantumCTek demonstrated 66 qubits with 113 photons : \*



\* Y. Wu *et al.*, *Phys. Rev. Lett.* **127**, 180501 (2021);

\*\* <https://www.sciencealert.com/china-s-latest-56-qubit-computer-marks-another-quantum-milestone>



# Trapped Ion Quantum Computer

Ionq introduced a quantum computer based on trapped ions : \*

**TECHNICAL DEMONSTRATION**

## Reconfigurable Multicore Quantum Architecture — 4x16

August 25, 2021



\* <https://ionq.com>;  
<https://www.youtube.com/watch?v=yvzU748e0V4>



# AI Chips

1.4 trillion transistors on a chip : \*

	WSE 2	WSE	Nvidia A100
Size	46,225 mm <sup>2</sup>	46,225 mm <sup>2</sup>	826 mm <sup>2</sup>
Transistors	2.6 trillion	1.2 trillion	54.2 billion
Cores	850,000	400,000	7,344
On-chip memory	40 gigabytes	18 GB	40 megabytes
Memory bandwidth	20 petabytes/s	9 PB/s	155 GB/s
Fabric bandwidth	220 petabits/s	100 Pb/s	600 gigabytes/s
Fabrication process	7 nm	16 nm	7 nm

\* <https://spectrum.ieee.org/cerebras-giant-ai-chip-now-has-a-trillions-more-transistors>