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Mixed-Criticality Job Models: A Comparison

Sanjoy Baruah and **Zhishan Guo**

Department of Computer Science

University of North Carolina at Chapel Hill

Mixed-Criticality Systems

- **MC Systems:** *functionalities* of different *levels of importance* (*criticalities*) are implemented upon a *shared platform*.



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- Traditional non-MC design:
Need significant **resource over-provisioning** to guarantee their **temporal correctness**, which leads to highly **inefficient resource usage** at run-time!



Mixed-Criticality Systems

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- Traditional non-MC design:
Need significant **resource over-provisioning** to guarantee their **temporal correctness**, which leads to highly **inefficient resource usage** at run-time!
- MC:
Over-provisioned resources (to more important tasks) can be used to execute less important ones.



Models



SAFETY-CRITICAL



**Temporal
Correctness**

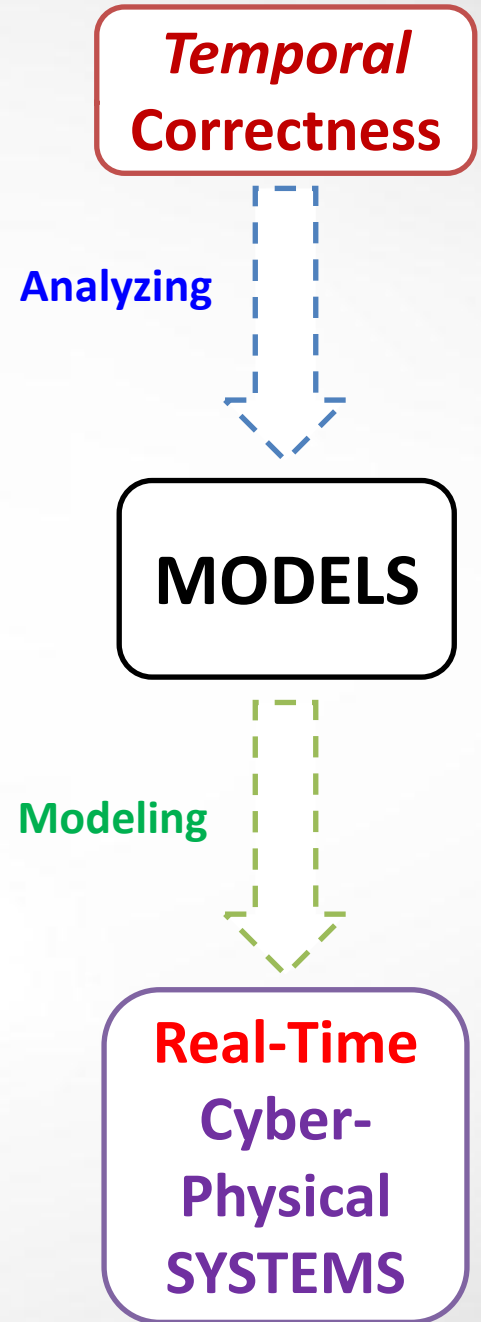


**Real-Time
Cyber-
Physical
SYSTEMS**

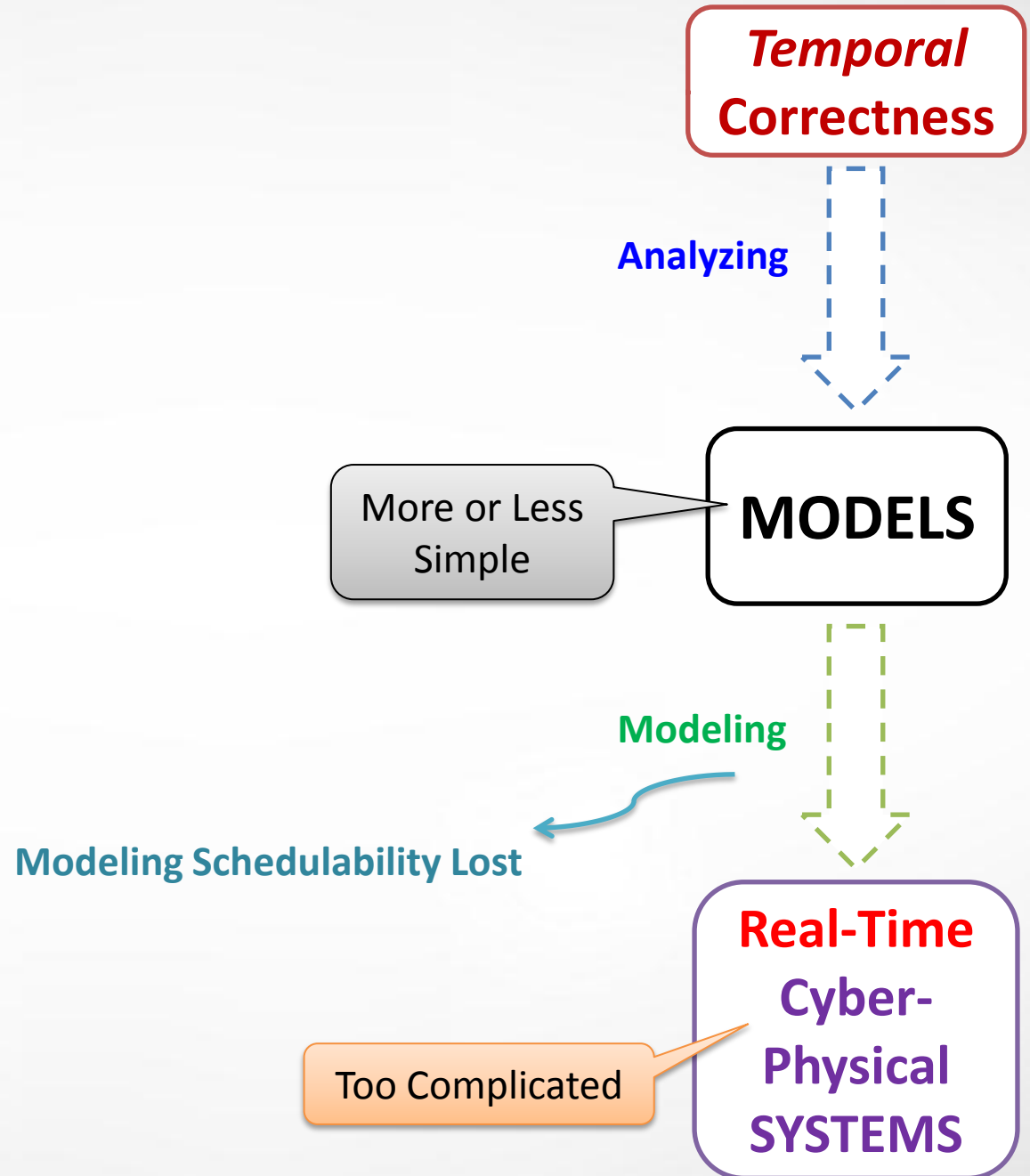


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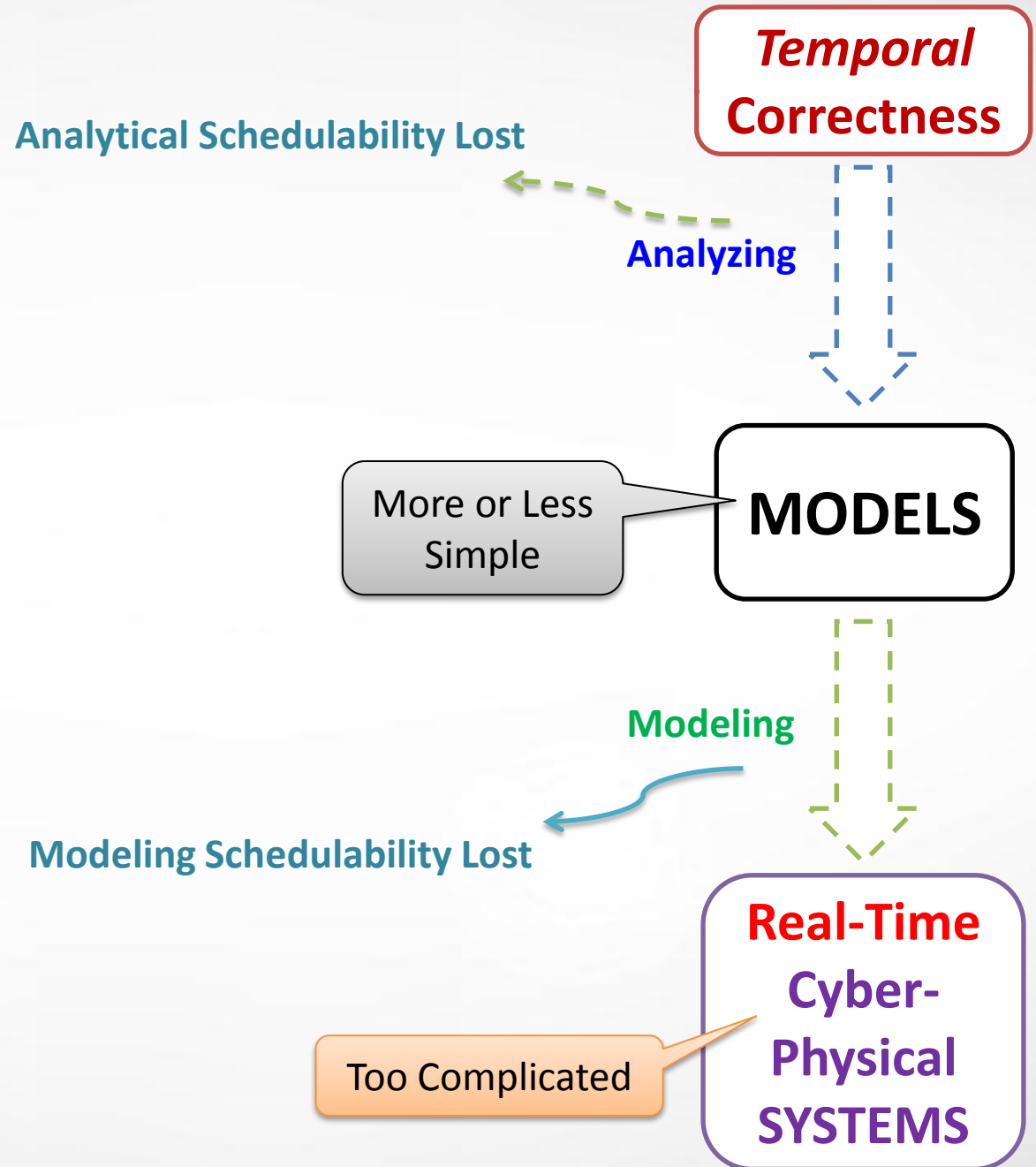
Models



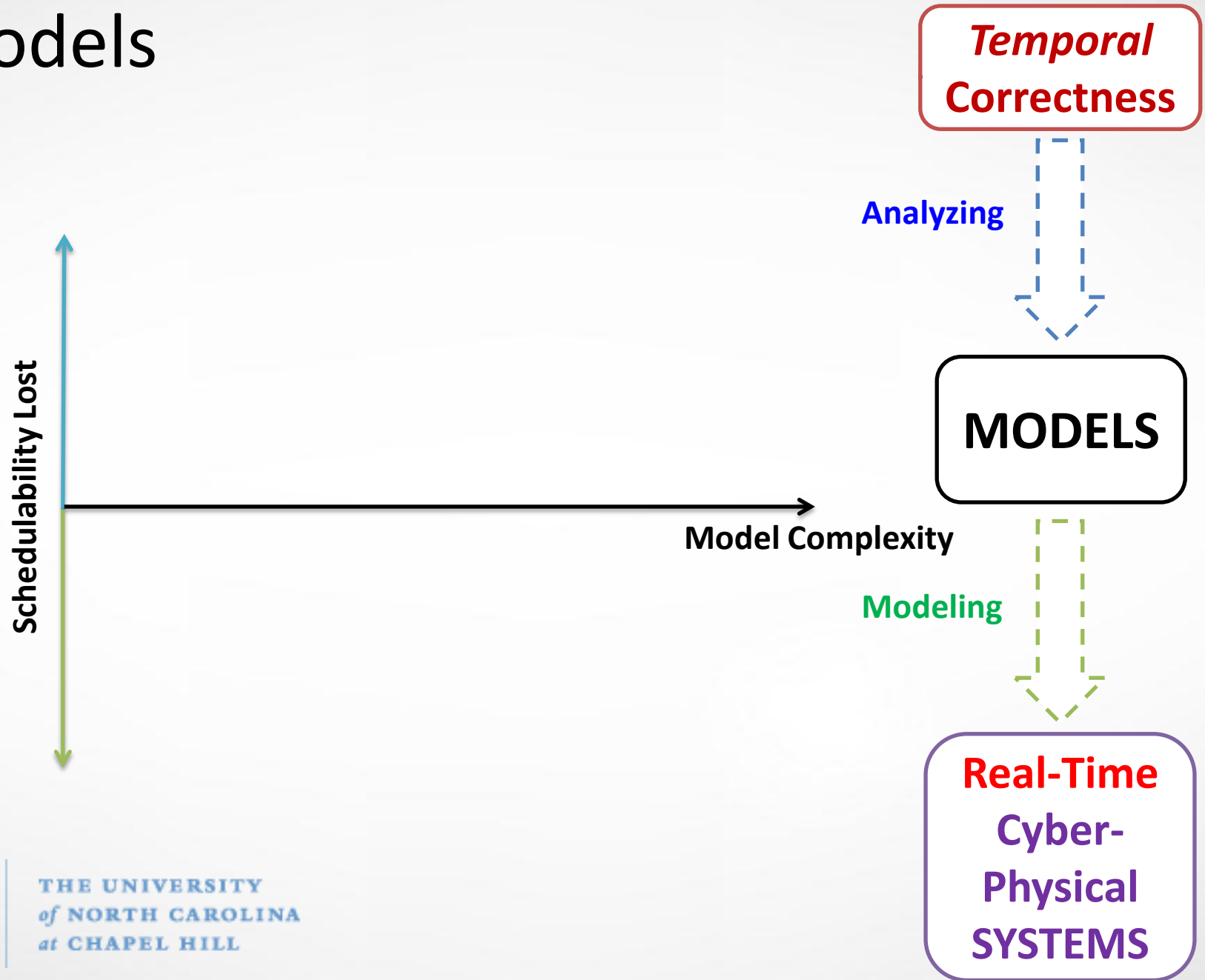
Models



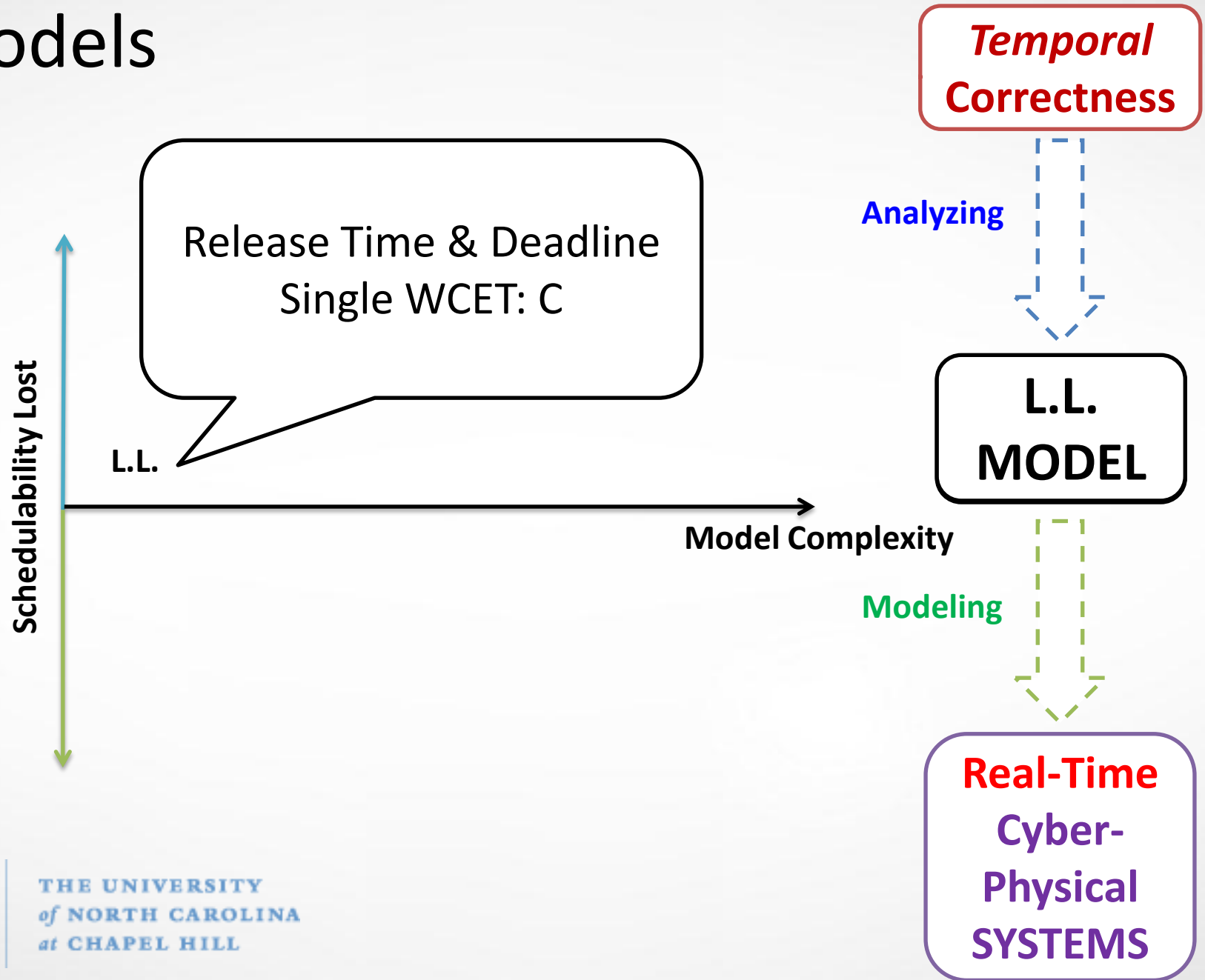
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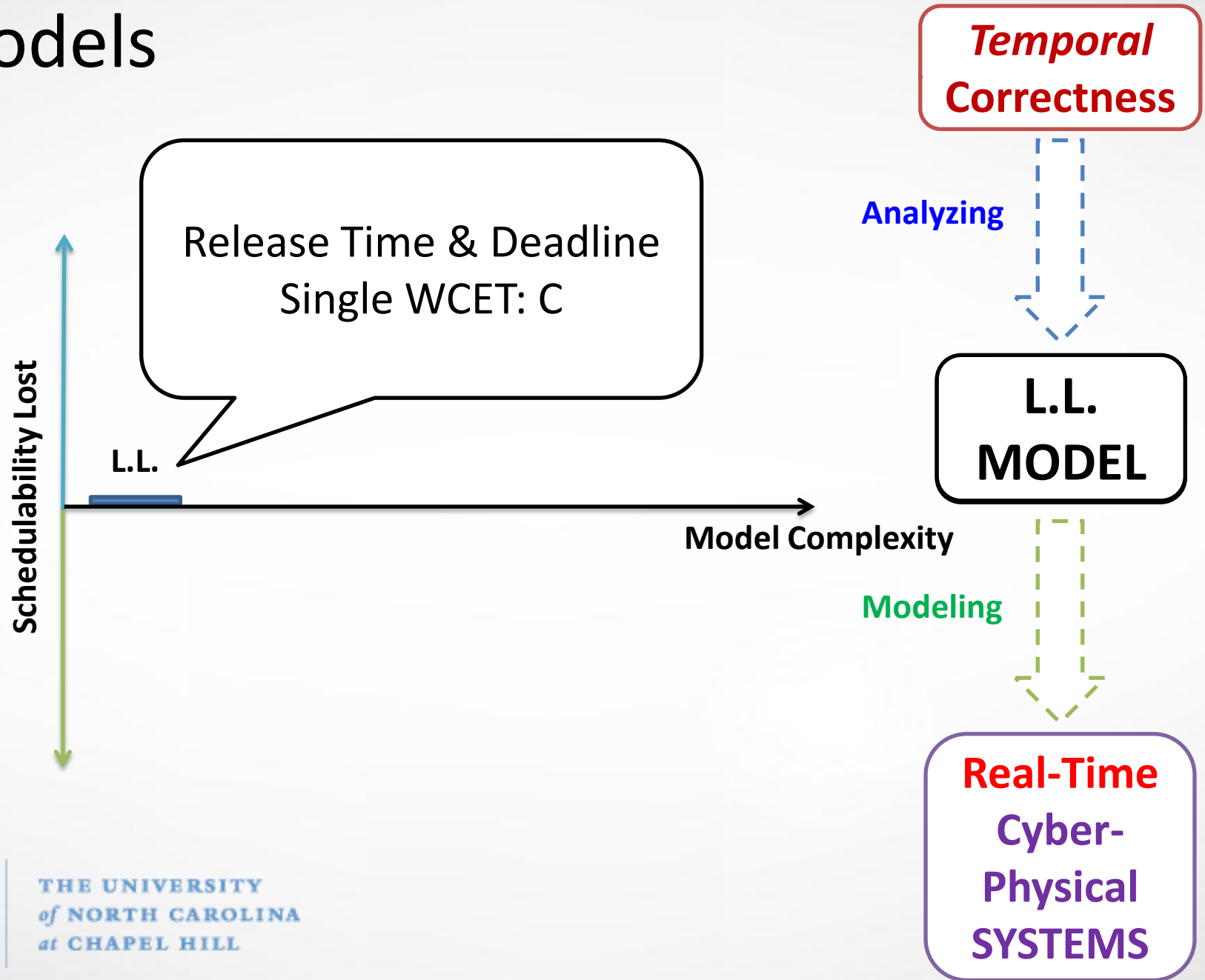
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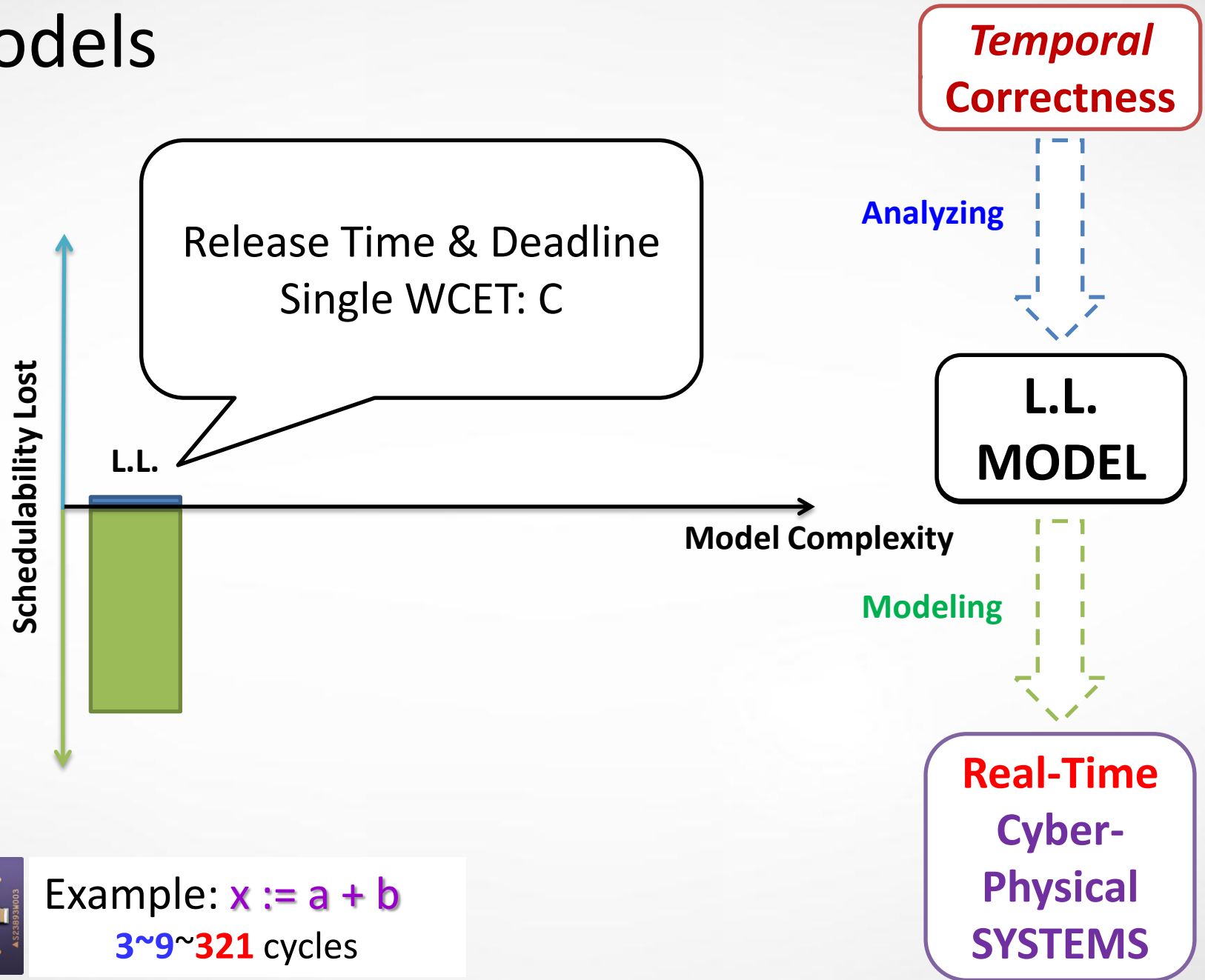
Models



Models

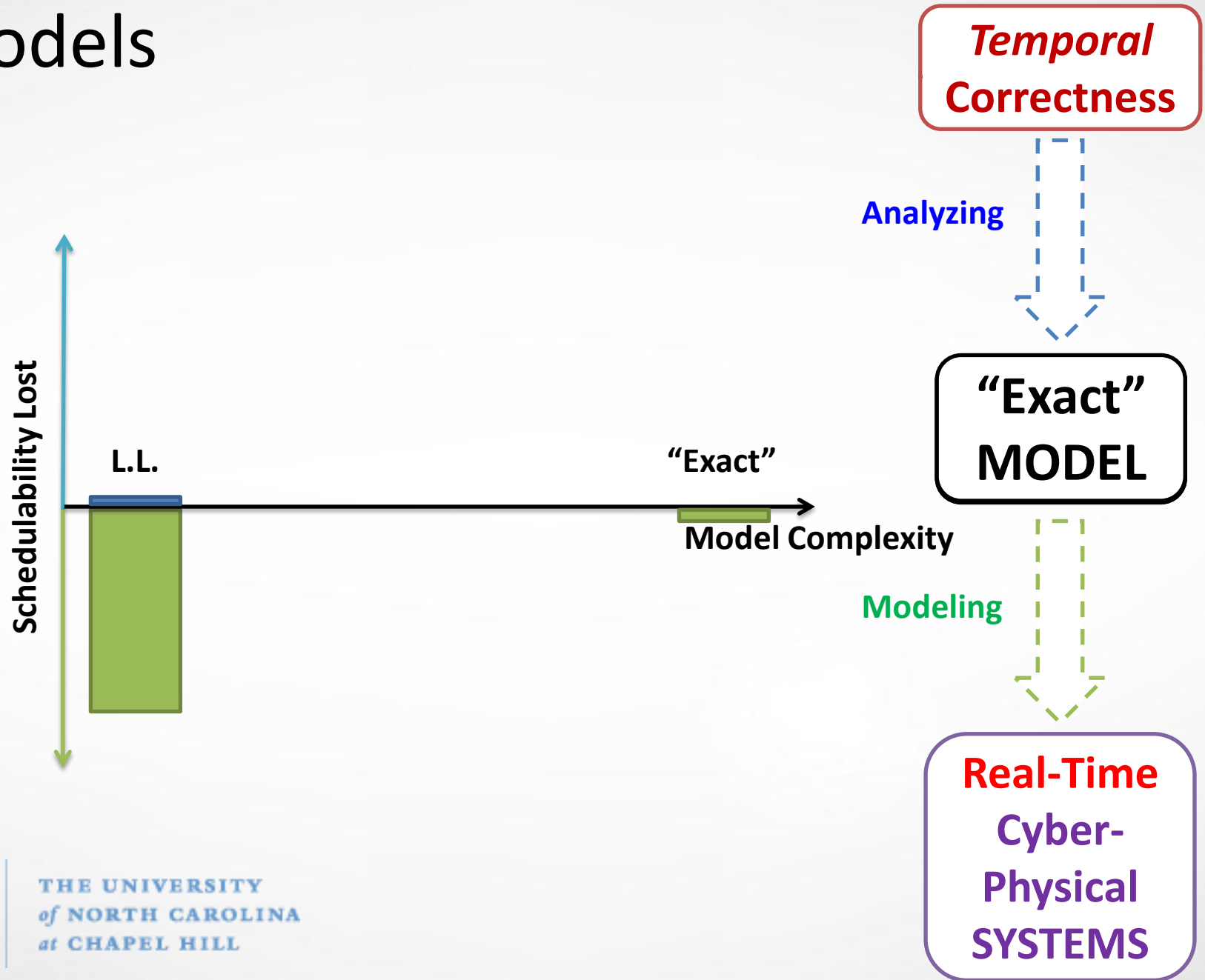


Models

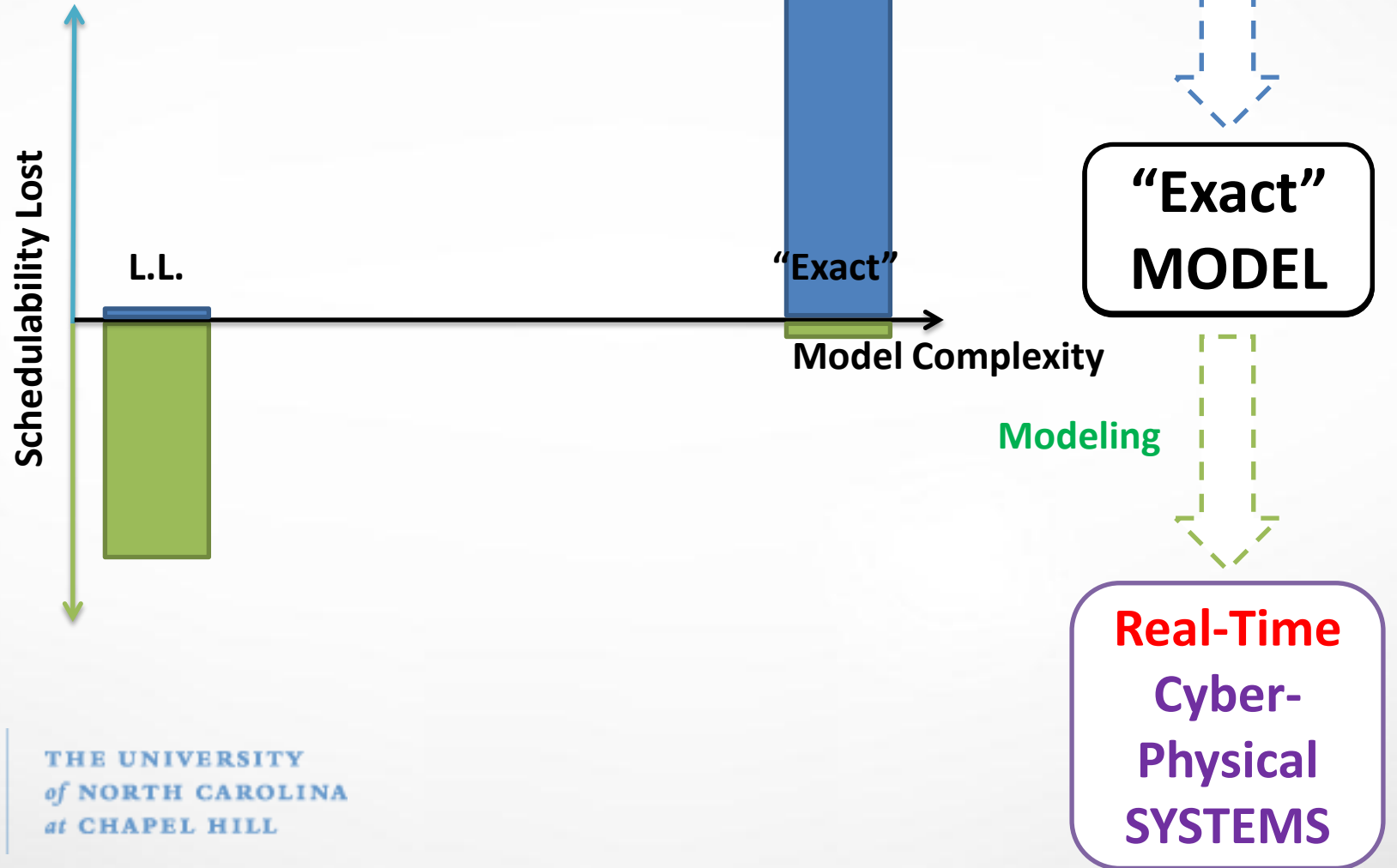


Example: $x := a + b$
3~9~321 cycles

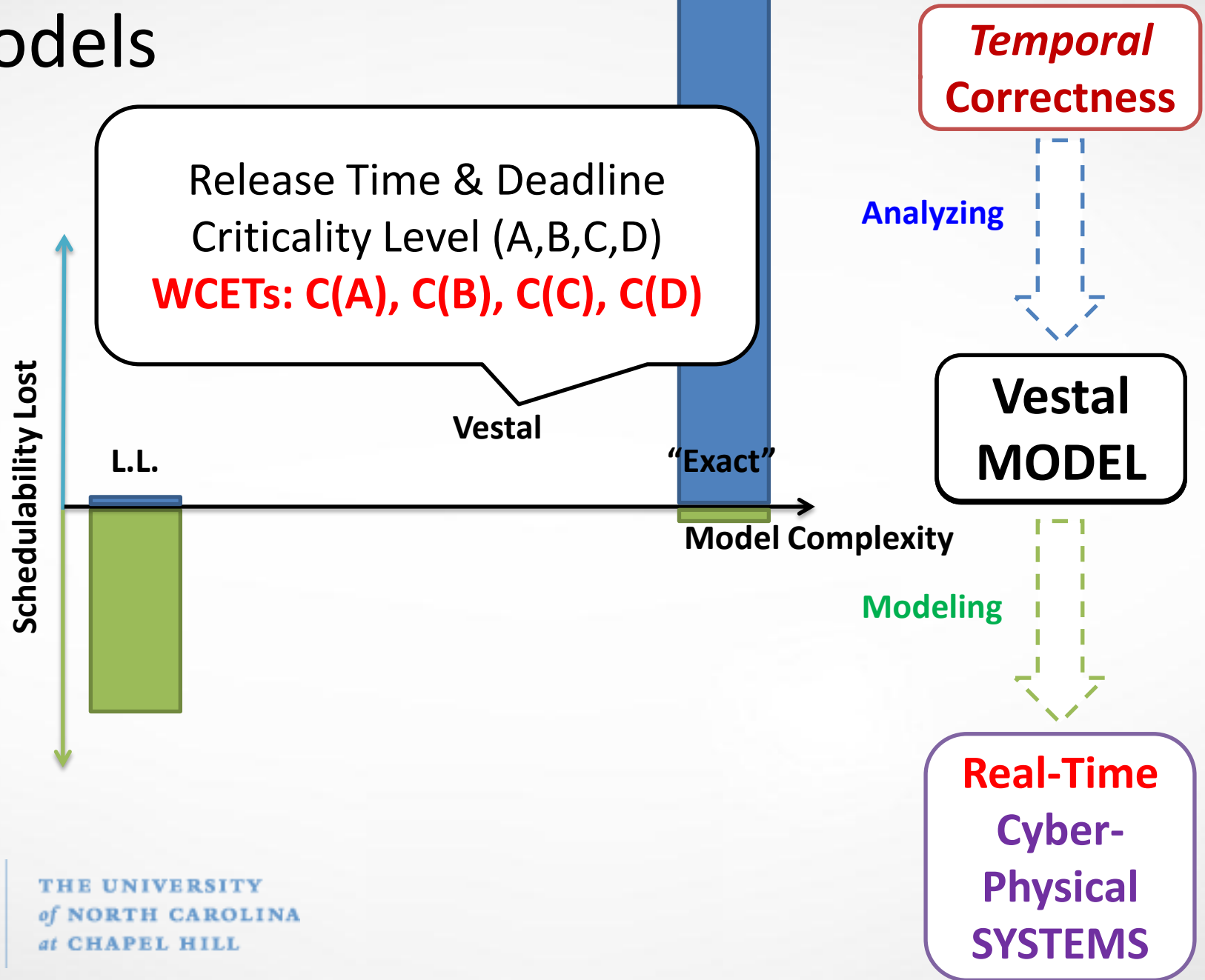
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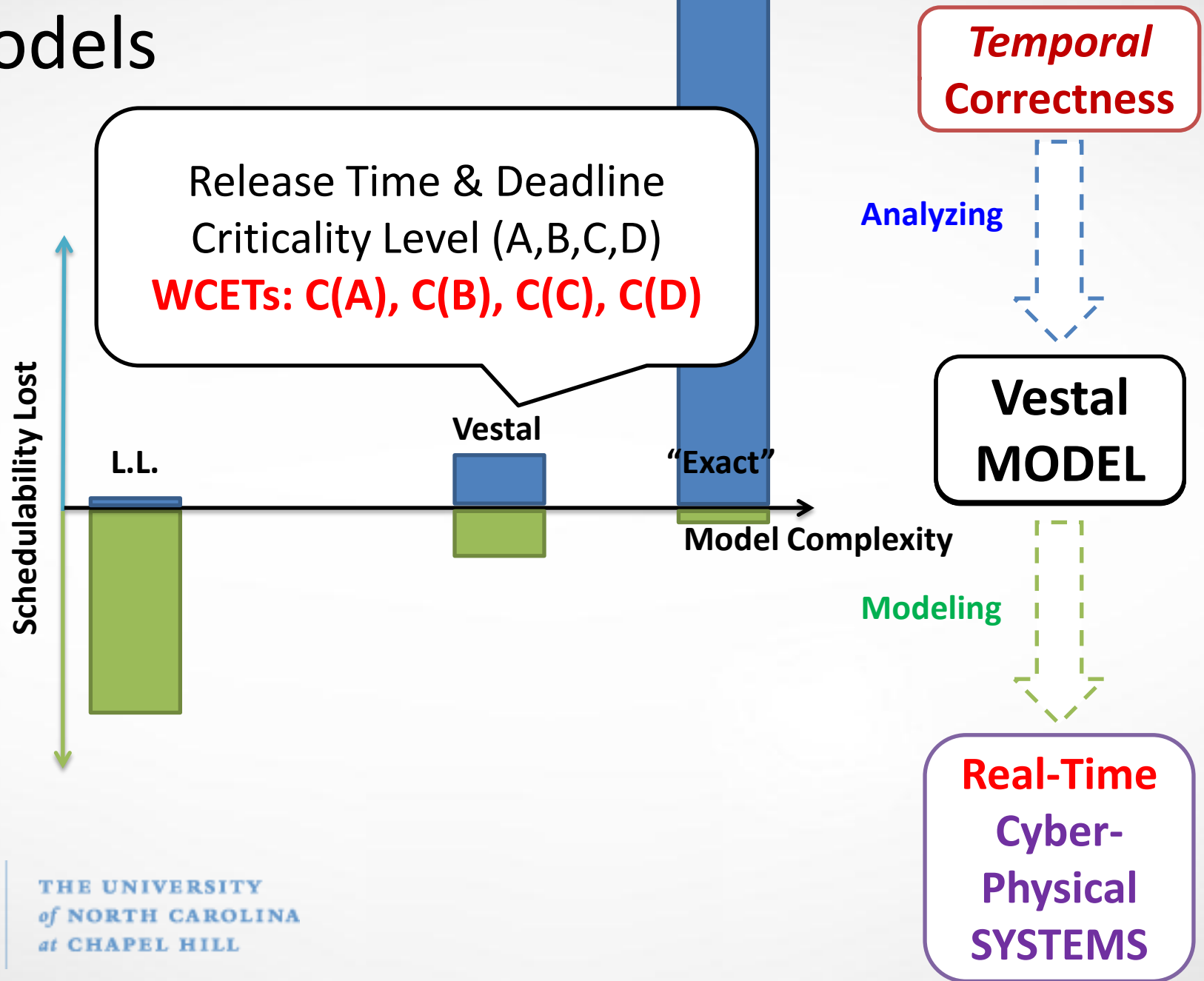
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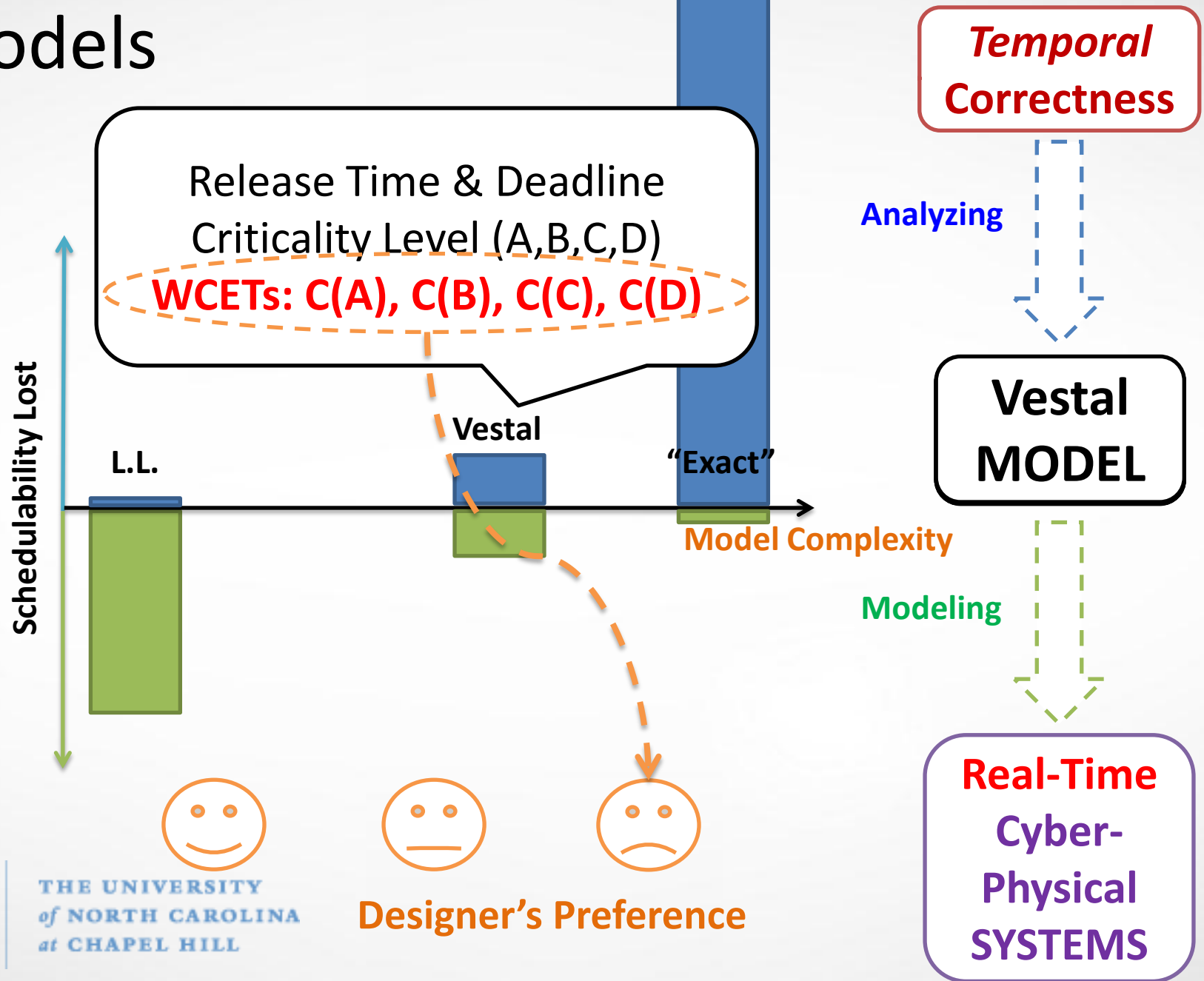
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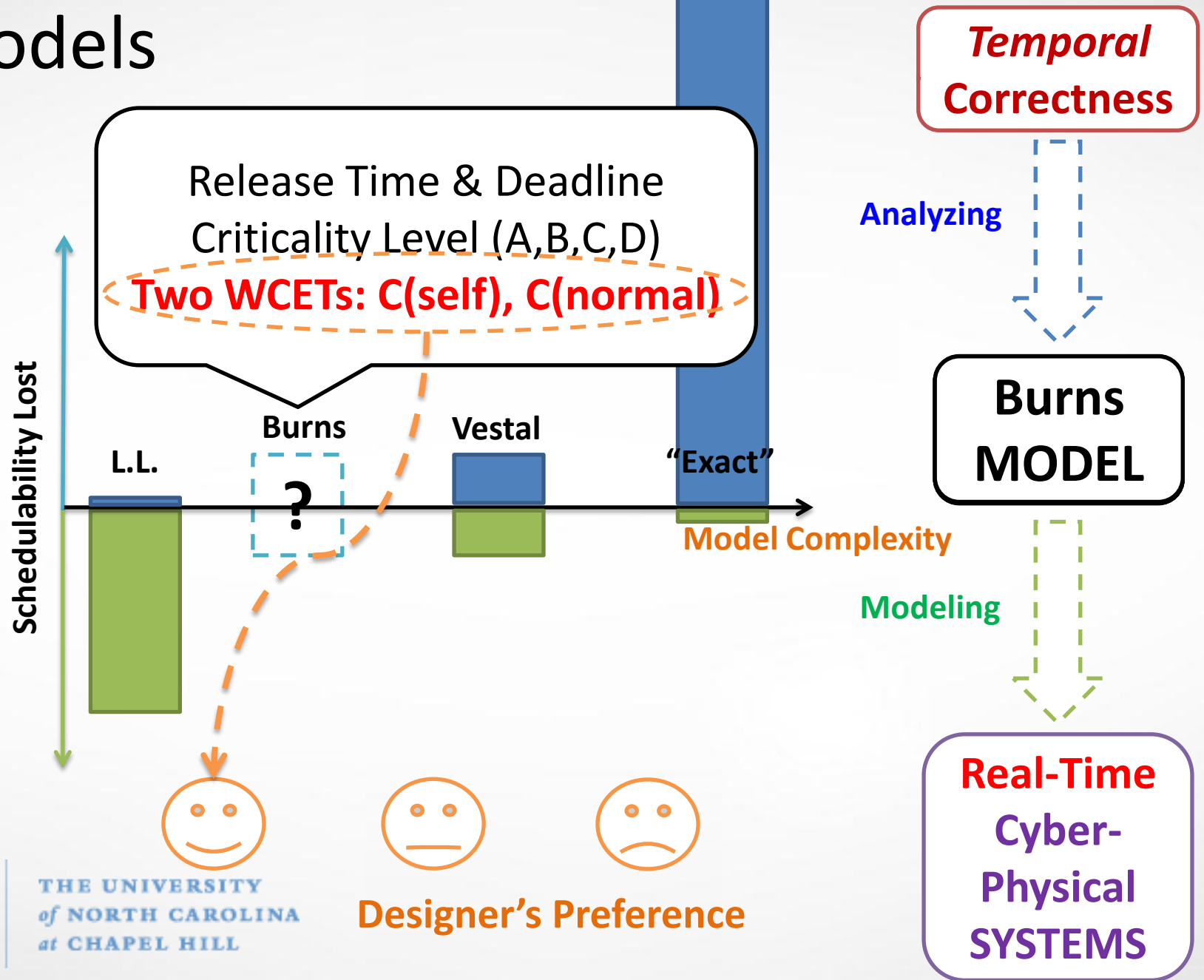
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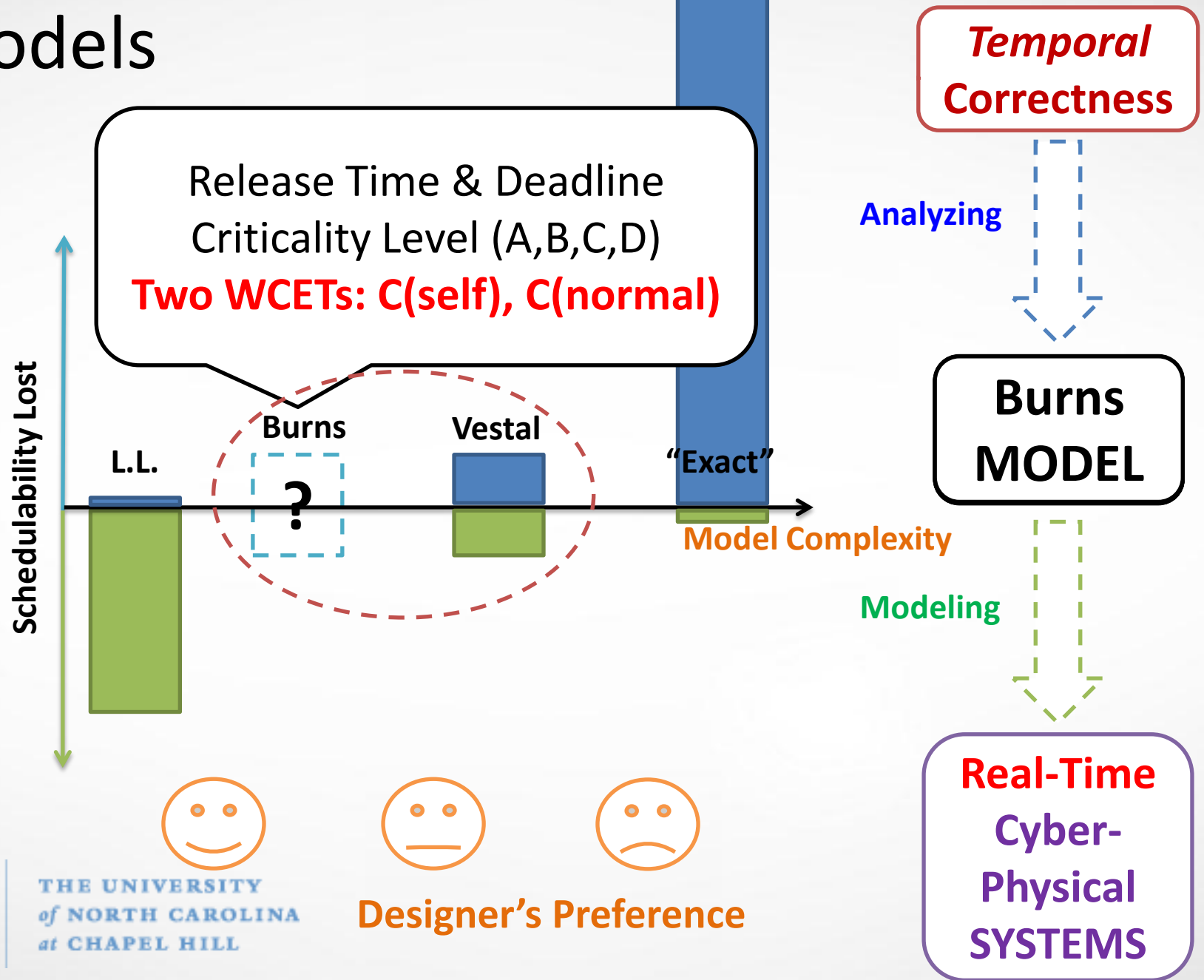
Models



Models



Models



Model Comparison

Vestal Model

Burns Model

Criticality Levels χ_i : **A**, **B**, **C**, or **D**

WCETs:

$C_i(\mathbf{A})$, **$C_i(\mathbf{B})$** , **$C_i(\mathbf{C})$** , **$C_i(\mathbf{D})$**
642, **321**, **10**, **5**

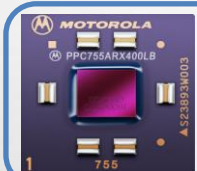


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3~9~**321** cycles

Model Comparison

<i>Vestal Model</i>	<i>Burns Model</i>
<i>Criticality Levels</i> χ_i : A , B , C , or D	
WCETs: $C_i(\mathbf{A})$, $C_i(\mathbf{B})$, $C_i(\mathbf{C})$, $C_i(\mathbf{D})$ 642 , 321 , 10 , 5	Only <u>Two</u> WCETs: $C_i(\mathbf{self})$, $C_i(\mathbf{normal})$ 642 , 5



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Example: $x := a + b$
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Actual execution time remains **unknown**
until the job *signals* its completion.
(**non-clairvoyant**)

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<p>Level of the System := Smallest ℓ that $C_i(\ell)$ caps behavior of job i, $\forall i$</p>	<p>Level of the System := χ_i of the greatest-criticality job exceeding its $C_i(\mathbf{NL})$</p>



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Vestal Model

*Temporal
Correctness
-- per level*

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N/A, **321**, **10**, **5**

Only **Two** WCETs:

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642, **5**, **5**, **5**

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642, **5**

Proposition 1:

Any instance represented in the Burns model
can be represented exactly in the Vestal model.



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N/A, **321**, **10**, **5**

Only Two WCETs:

$C_i(SF)$, **$C_i(NL)$**
321, **5**

Proposition 2:

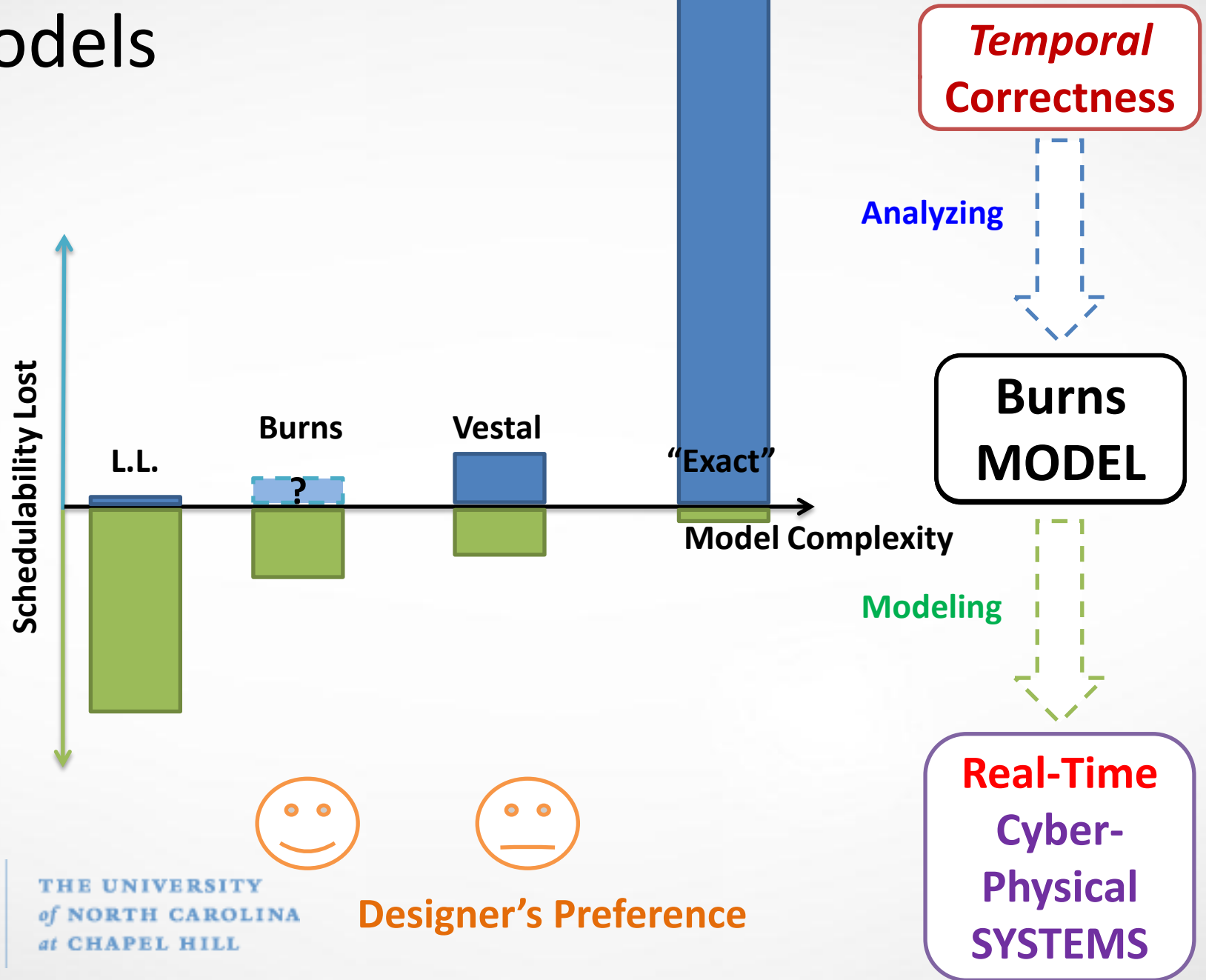
Instances represented in the Vestal model
cannot always be represented exactly in the Burns model.



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Models

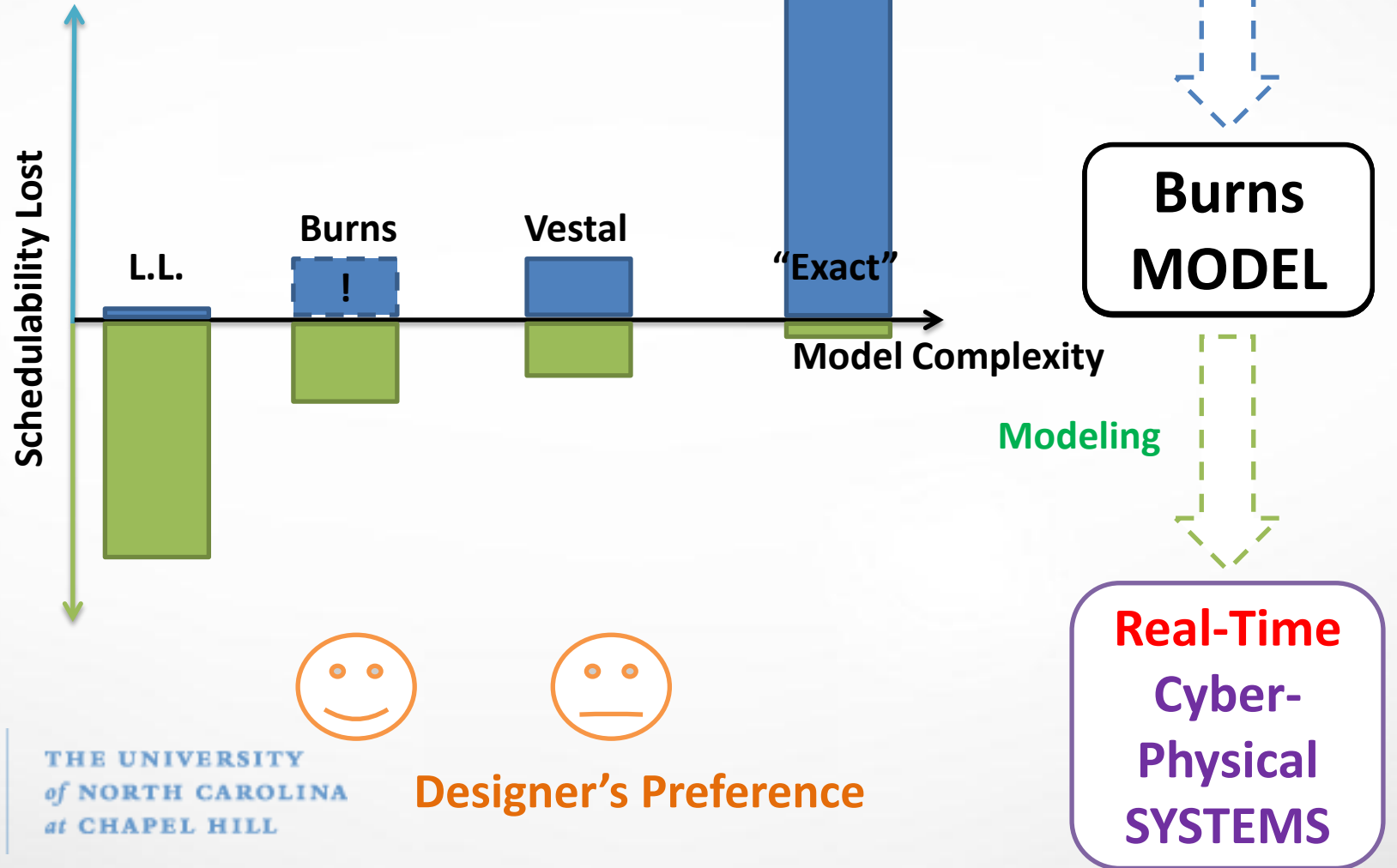


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Designer's Preference

Real-Time
Cyber-
Physical
SYSTEMS

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Proposition 3:

Determining whether a given instance specified according to the Burns model is MC-schedulable is NP-hard in s.s.



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Thm 1:

There are MC instances with L distinct criticality levels specified using the Burns model that are clairvoyantly-schedulable, but that are not schedulable for any fixed priority policy on a processor that is less than s_L^* times as fast.

* s^L is the root of $x^L = (1 + x)^{L-1}$, i.e., the speedup bound under Vestal model.

Conclusion

- We seek to better understand the Ease-of-use Burns model.
- Unfortunately, we have not identified any analytical benefits in terms of reduced complexity of feasibility analysis, less schedulability loss, etc., at the cost of reduced expressiveness.



Conclusion & Future Work

- We seek to better understand the Ease-of-use Burns model.
- Unfortunately, we have not identified any analytical benefits in terms of reduced complexity of feasibility analysis, less schedulability loss, etc., at the cost of reduced expressiveness.
- Limitation: Fixed-Priority; Job Set; Uniprocessor.





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Thank you!

Zhishan Guo

zsguo@cs.unc.edu

WMC'15, San Antonio