

# Time-Triggered Mixed-Critical Scheduler <sup>1</sup>

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Verimag - Université Joseph Fourier - Grenoble

Workshop on Mixed Criticality Systems

<sup>1</sup>The research leading to these results has received funding from the European Community's Seventh Framework Programme [FP7/2007-2013] under grant agreement no. 288175 [Certainty].

# Schedulability

## in Dual Critical Systems

- scheduling is a major challenge of Mixed Critical System design
- **finite** set of jobs in **dual critical systems**:
  - every job is classified as critical (HI) or non-critical (LO)
  - every job is labeled with two Worst Case Execution Times:
    - LO WCET computed with industrial standard tools  
(realistic estimation)
    - HI WCET computed with Certification Authority tools  
(very pessimistic estimation)
  - both HI and LO jobs are Hard Real-Time

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- the scheduling problem is NP-complete



# Basic scenario

- an execution where all jobs terminates after executing for  $C(LO)$  before a *switch time*  $t_s$  and for  $C(HI)$  after  $t_s$  is called **basic scenario**
- analyzing **basic scenario** is enough
- we call a basic scenario  $LO$  if no jobs run for  $C(HI)$   
 $HI - J_s$  if  $J_s$  is the first job to execute for more than  $C(LO)$

# Example of scheduling problem

- Let us apply different scheduling to the instance:

Job	A	D	$\chi$	$C(LO)$	$C(HI)$
1	0	1	LO	1	1
2	0	3	LO	1	1
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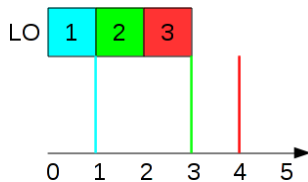
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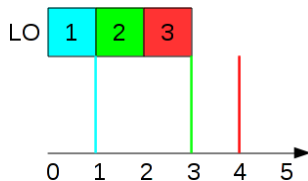


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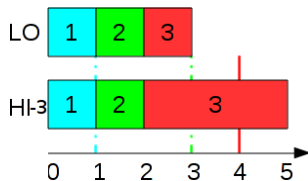
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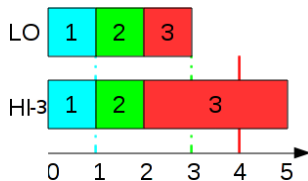
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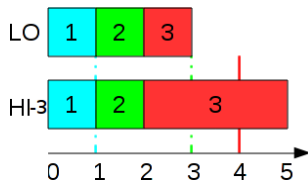
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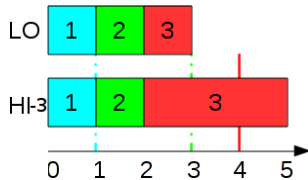


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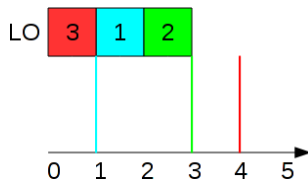
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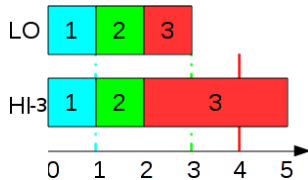
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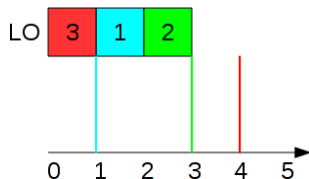
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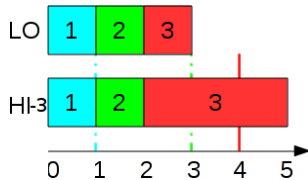
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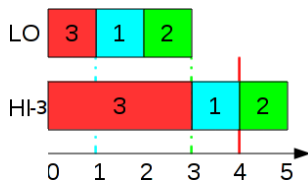
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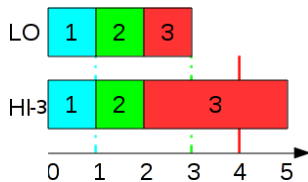
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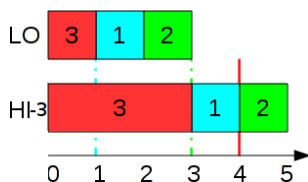
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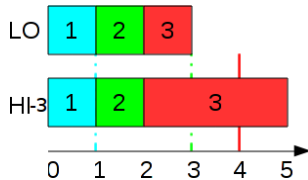
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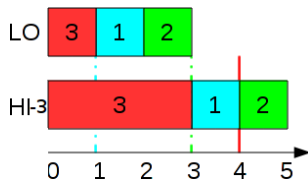
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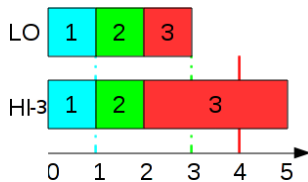
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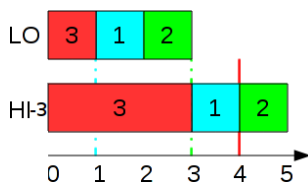
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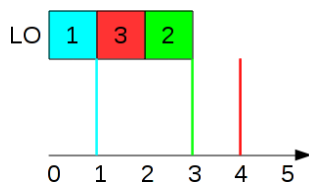
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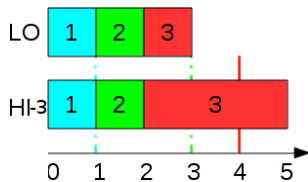
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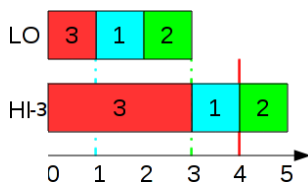
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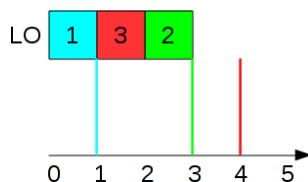
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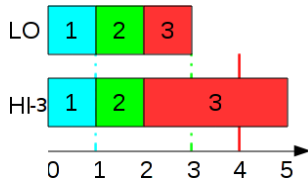
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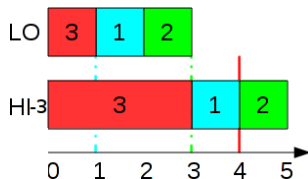
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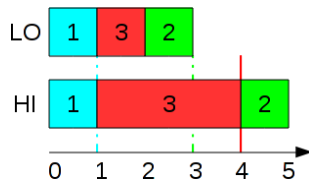
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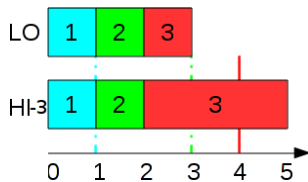


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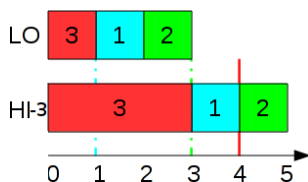
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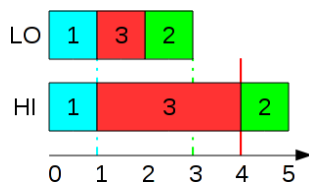
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- Single Time Table per Mode (STTM)[1]
  - one TT table per criticality mode

[1] S. Baruah and G. Fohler. “Certification-Cognizant Time-Triggered Scheduling of Mixed-Criticality Systems”. In: *Real-Time Systems Symposium (RTSS), 2011 IEEE 32nd*.

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$$\text{Alg: } FPM \mapsto STTM$$

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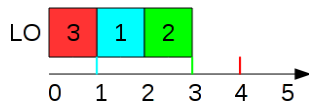
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STTM scheduling defined by two TT table **LO** and **HI\***
- We generate table **LO** by simulating the execution of the LO scenario

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# The algorithm

## generation of HI\*

- Let at time  $t$ :
  - $T_j^{LO}(t)$  (resp.  $T_j^{HI^*}(t)$ ) = progress of  $J_j$  in **LO** (resp. **HI\***)
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Generate **HI\*** by simulation of HI jobs:

- each job executes for  $C(HI)$  time units
- the jobs are scheduled according to  $PT_{HI}$
- a job is enabled by one of the following *rules*:

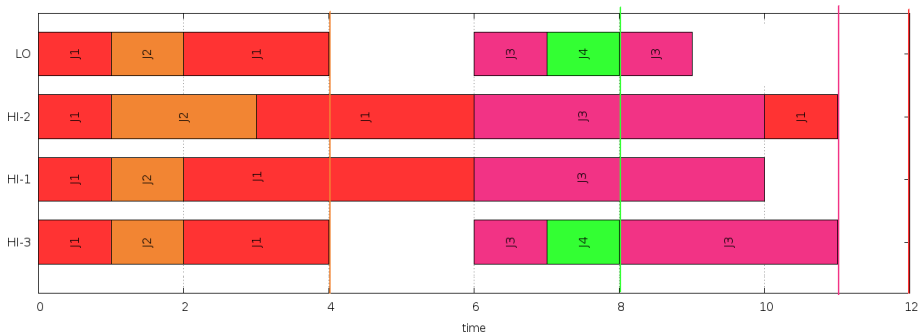
$$\begin{aligned}
 T_j^{LO}(t) &= C_j(\text{LO}) \\
 T_j^{HI^*}(t) &< T_j^{LO}(t) \\
 T_j^{HI^*}(t) &= T_j^{LO}(t) \wedge E^{LO}(t) = J_j
 \end{aligned}$$

# Example

Job	A	D	$\chi$	C(LO)	C(HI)
1	0	12	HI	3	5
2	1	4	HI	1	2
3	6	11	HI	2	4
4	7	8	LO	1	1

$$PT_{LO} = J_4 \succ J_2 \succ J_3 \succ J_1$$

$$PT_{HI} = J_2 \succ J_3 \succ J_1$$





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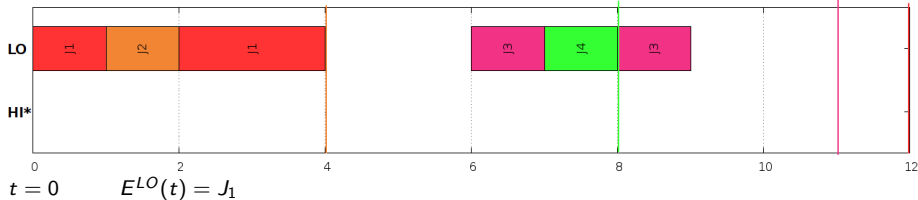
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Job	STATUS	$T^{HI^*}(t)$	$T^{LO}(t)$	$C(\text{LO})$	$C(\text{HI})$	(1)	(2)	(3)
1	Enabled	0	0	3	5			✓
2								
3								

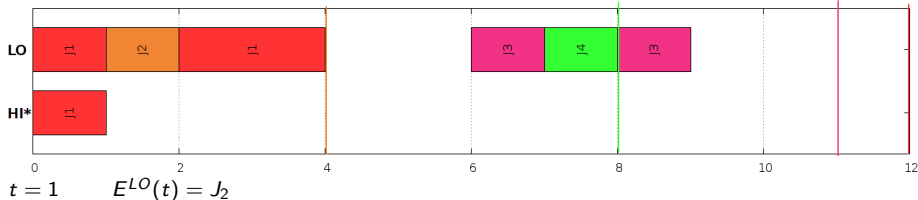
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Job	STATUS	$T^{HI*}(t)$	$T^{LO}(t)$	$C(LO)$	$C(HI)$	(1)	(2)	(3)
1	Disabled	1	1	3	5			
2	Enabled	0	0	1	2			✓
3								

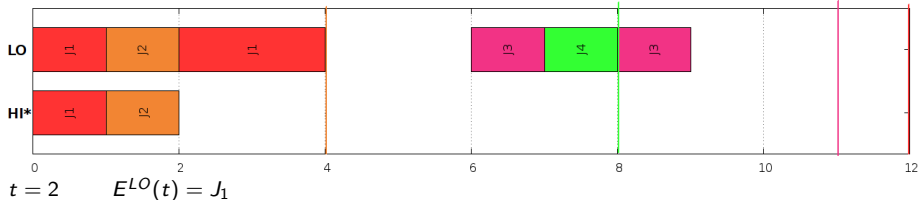
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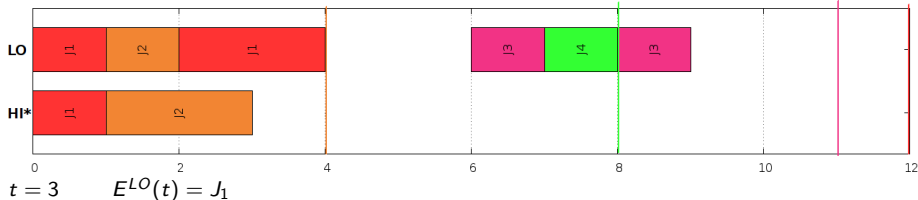
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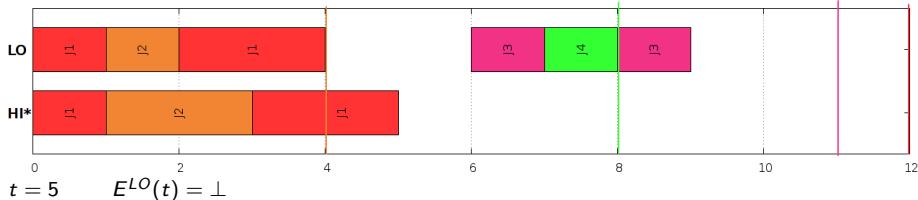
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$$T_j^{HI*}(t) < T_j^{LO}(t) \quad (2)$$

$$T_j^{HI*}(t) = T_j^{LO}(t) \wedge E^{LO}(t) = J_j \quad (3)$$



Job	STATUS	$T^{HI*}(t)$	$T^{LO}(t)$	$C(LO)$	$C(HI)$	(1)	(2)	(3)
1	Enabled	3	3	3	5	✓		
2	Term.	2	1	1	2			
3								

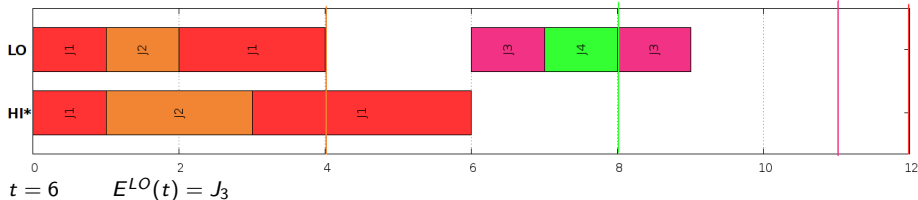
## Example

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Job	STATUS	$T^{HI*}(t)$	$T^{LO}(t)$	$C(LO)$	$C(HI)$	(1)	(2)	(3)
1	Enabled	4	3	3	5	✓		
2	Term.	2	1	1	2			
3	Enabled	0	0	2	4			✓

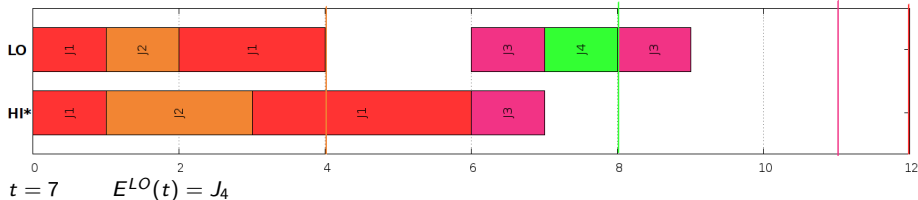
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Job	STATUS	$T^{HI*}(t)$	$T^{LO}(t)$	$C(LO)$	$C(HI)$	(1)	(2)	(3)
1	Enabled	4	3	3	5	✓		
2	Term.	2	1	1	2			
3	Disabled	1	1	2	4			



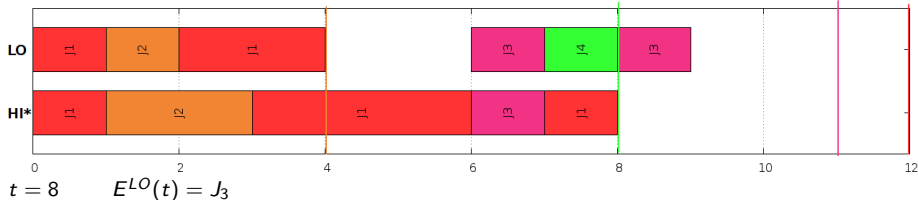
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Job	STATUS	$T^{HI^*}(t)$	$T^{LO}(t)$	$C(LO)$	$C(HI)$	(1)	(2)	(3)
1	Term.	5	3	3	5			
2	Term.	2	1	1	2			
3	Enabled	1	1	2	4			✓

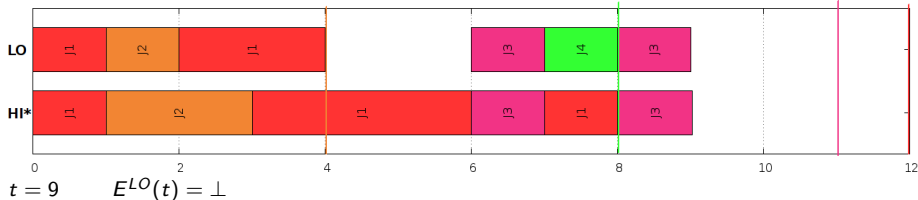
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1	Term.	5	3	3	5			
2	Term.	2	1	1	2			
3	Enabled	2	1	2	4	✓		

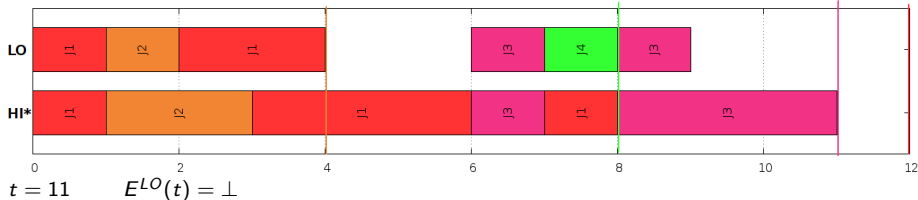
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1	Term.	5	3	3	5			
2	Term.	2	1	1	2			
3	Term.	4	1	2	4			

# Proof of correctness

## Theorem

*If the FPM policy leads to a feasible schedule, then a switched time triggered schedule that uses **LO** and **HI\*** as, respectively, LO-mode and HI-mode table, is a feasible schedule as well.*

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## Lemma

*If at any time we switch from **LO** to **HI\***, then all the unterminated jobs will have enough time reserved in **HI\*** to terminate their work.*

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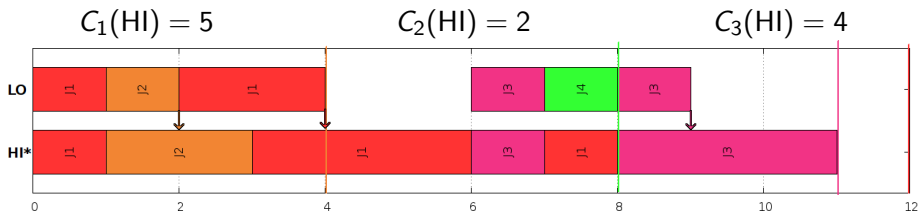
*For all HI jobs  $J$  there exists a basic scenario of the FPM scheduling where  $J$  terminates no earlier than in **HI\****

# correctness of example

It is easy to show that the lemma is true for our example

## Lemma

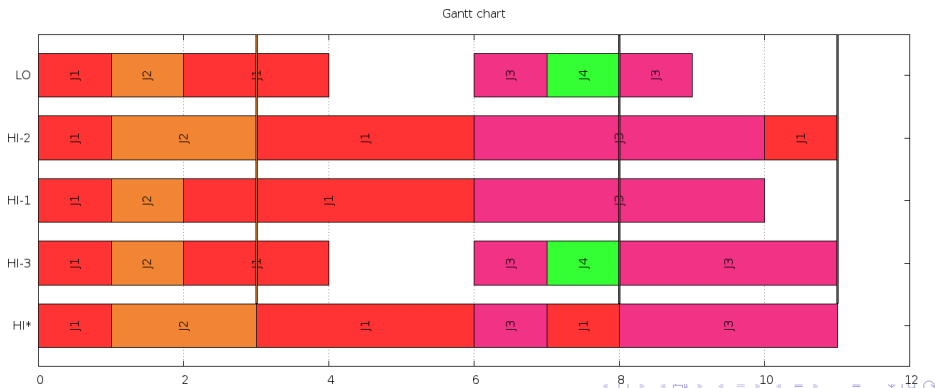
*If at any time we switch from **LO** to **HI\***, then all the unterminated jobs will have enough time reserved in **HI\*** to terminate their work.*



# correctness of example

## Theorem

*For all HI jobs  $J$  there exists a basic scenario of the FPM scheduling where  $J$  terminates no earlier than in  $\mathbf{HI}^*$*





- Conclusions

- Proof that  $FPM \subset STTM$
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- Future work

- More than two criticality levels
- Multiprocessor